

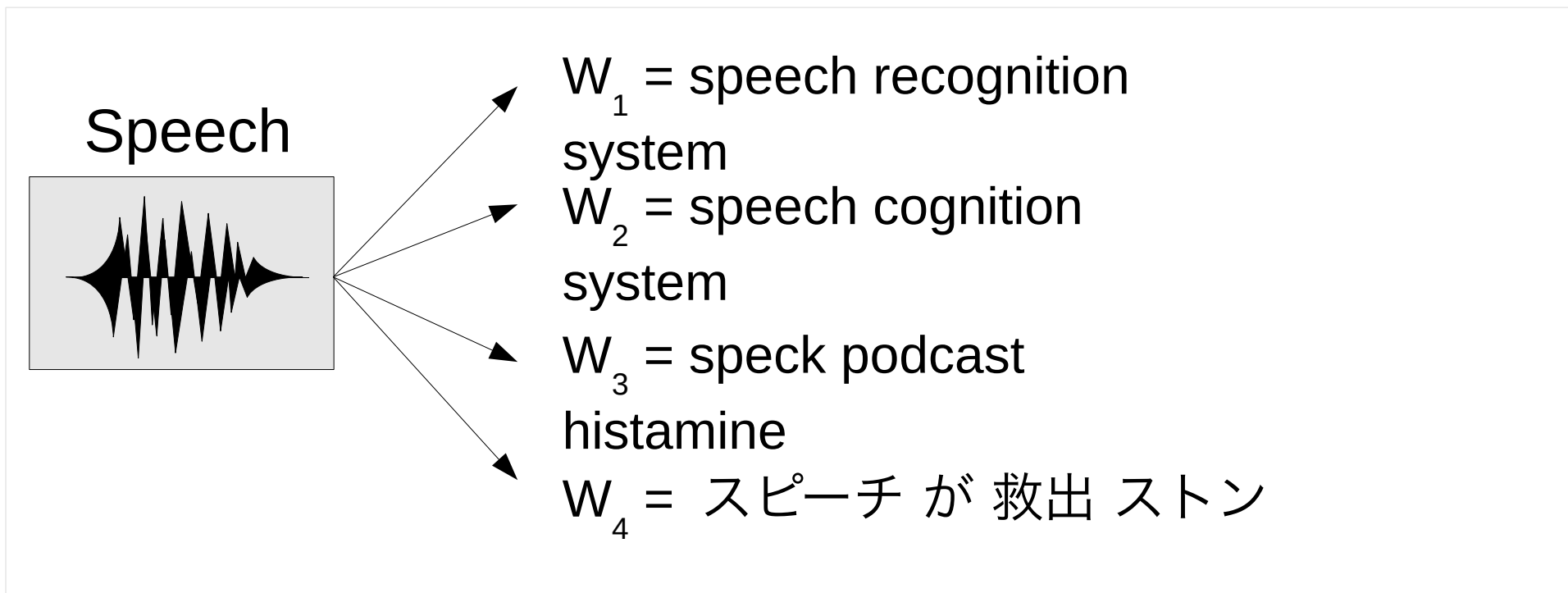
NLP Programming Tutorial 1 - Unigram Language Models

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Language Model Basics

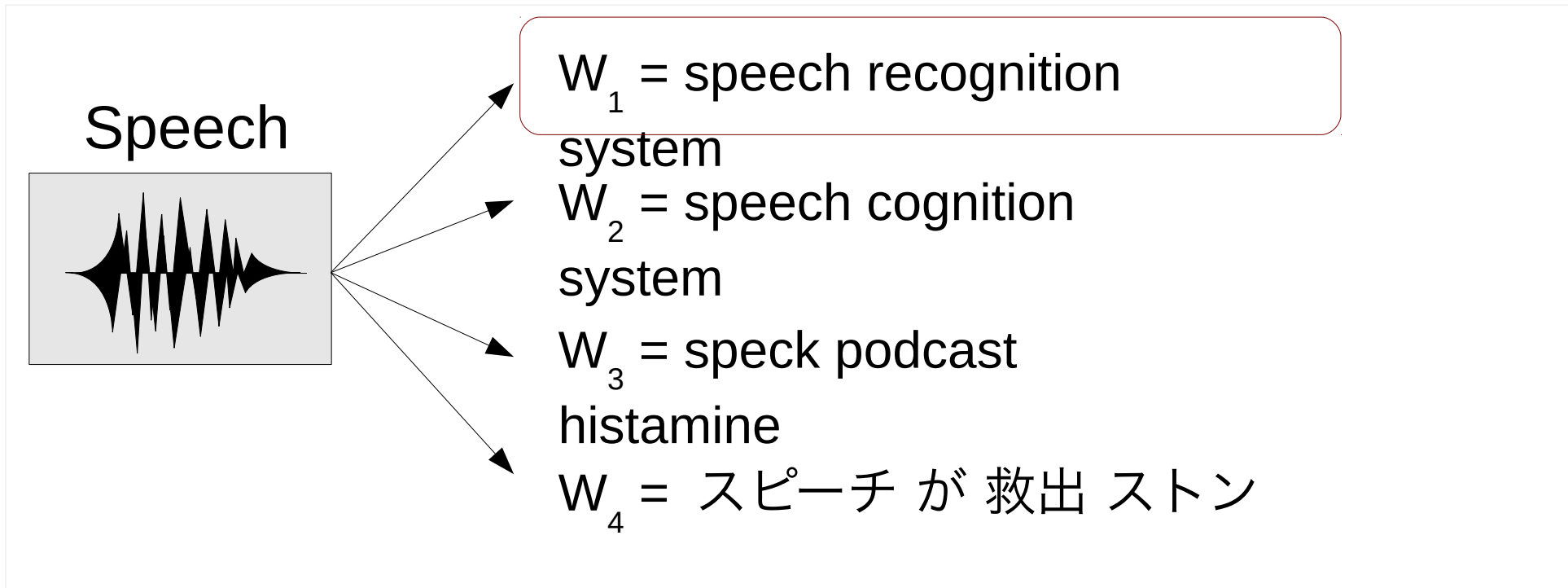
Why Language Models?

- We have an English speech recognition system, which answer is better?



Why Language Models?

- We have an English speech recognition system, which answer is better?



- Language models tell us the answer!

Probabilistic Language Models

- Language models assign a probability to each sentence

W_1 = speech recognition
system

$$P(W_1) = 4.021 * 10^{-3}$$

W_2 = speech cognition
system

$$P(W_2) = 8.932 * 10^{-4}$$

W_3 = speck podcast
histamine

$$P(W_3) = 2.432 * 10^{-7}$$

W_4 = スピーチ が 救出 ストン

$$P(W_4) = 9.124 * 10^{-23}$$

- We want $P(W_1) > P(W_2) > P(W_3) > P(W_4)$
 - (or $P(W_4) > P(W_1), P(W_2), P(W_3)$ for Japanese?)

Calculating Sentence Probabilities

- We want the probability of

$W = \text{speech recognition system}$

- Represent this mathematically as:

$$P(|W| = 3, w_1 = \text{"speech"}, w_2 = \text{"recognition"}, w_3 = \text{"system"})$$

Calculating Sentence Probabilities

- We want the probability of

W = speech recognition system

- Represent this mathematically as (using chain rule):

$$P(|W| = 3, w_1 = \text{"speech"}, w_2 = \text{"recognition"}, w_3 = \text{"system"}) =$$

$$P(w_1 = \text{"speech"} \mid w_0 = \text{"<s>"})$$

$$* P(w_2 = \text{"recognition"} \mid w_0 = \text{"<s>"}, w_1 = \text{"speech"})$$

$$* P(w_3 = \text{"system"} \mid w_0 = \text{"<s>"}, w_1 = \text{"speech"}, w_2 = \text{"recognition"})$$

$$* P(w_4 = \text{"</s>"} \mid w_0 = \text{"<s>"}, w_1 = \text{"speech"}, w_2 = \text{"recognition"}, w_3 = \text{"system"})$$

NOTE:

sentence start <s> and end </s> symbol

NOTE:

$$P(w_0 = \text{"<s>"}) = 1$$

Incremental Computation

- Previous equation can be written:

$$P(W) = \prod_{i=1}^{|W|+1} P(w_i | w_0 \dots w_{i-1})$$

- How do we decide probability?

$$P(w_i | w_0 \dots w_{i-1})$$

Maximum Likelihood Estimation

- Calculate word strings in corpus, take fraction

$$P(w_i | w_1 \dots w_{i-1}) = \frac{c(w_1 \dots w_i)}{c(w_1 \dots w_{i-1})}$$

i **live** in osaka . </s>

i **am** a graduate student . </s>

my school is in nara . </s>

$$P(\text{live} | \langle s \rangle i) = c(\langle s \rangle i \text{ live}) / c(\langle s \rangle i) = 1 / 2 = 0.5$$

$$P(\text{am} | \langle s \rangle i) = c(\langle s \rangle i \text{ am}) / c(\langle s \rangle i) = 1 / 2 = 0.5$$

Problem With Full Estimation

- Weak when counts are low:

Training:

i live in osaka . </s>
i am a graduate student . </s>
my school is in nara . </s>

Test:

<s> i live in nara . </s>



$$P(\text{nara} | \text{<s> i live in}) = 0/1 = 0$$



$$P(W = \text{<s> i live in nara . </s>}) = 0$$

Unigram Model

- Do not use history:

$$P(w_i | w_1 \dots w_{i-1}) \approx P(w_i) = \frac{c(w_i)}{\sum_{\tilde{w}} c(\tilde{w})}$$

i live in osaka . </s>

i am a graduate student . </s>

my school is in nara . </s>

$$P(\text{nara}) = 1/20 = 0.05$$

$$P(\text{i}) = 2/20 = 0.1$$

$$P(\text{</s>}) = 3/20 = 0.15$$

$$P(W=\text{i live in nara . </s>}) =$$

$$0.1 * 0.05 * 0.1 * 0.05 * 0.15 * 0.15 = 5.625 * 10^{-7}$$

Be Careful of Integers!

- Divide two integers, you get an integer (rounded down)

```
first_int = 1
second_int = 2
```

```
print(first_int/second_int)
```

```
$ ./my-program.py
0
```

- Convert one integer to a float, and you will be OK

```
print(float(first_int)/second_int)
```

```
$ ./my-program.py
0.5
```

What about Unknown Words?!

- Simple ML estimation doesn't work

i live in osaka . </s>		$P(\text{nara}) = 1/20 = 0.05$
i am a graduate student . </s>	→	$P(i) = 2/20 = 0.1$
my school is in nara . </s>		$P(\text{kyoto}) = 0/20 = 0$

- Often, unknown words are ignored (ASR)
- Better way to solve
 - Save some probability for unknown words ($\lambda_{\text{unk}} = 1 - \lambda_1$)
 - Guess total vocabulary size (N), including unknowns

$$P(w_i) = \lambda_1 P_{ML}(w_i) + (1 - \lambda_1) \frac{1}{N}$$

Unknown Word Example

- Total vocabulary size: $N=10^6$
- Unknown word probability: $\lambda_{\text{unk}}=0.05$ ($\lambda_1 = 0.95$)

$$P(w_i) = \lambda_1 P_{ML}(w_i) + (1 - \lambda_1) \frac{1}{N}$$

$$P(\text{nara}) = 0.95 * 0.05 + 0.05 * (1/10^6) = 0.047500005$$

$$P(i) = 0.95 * 0.10 + 0.05 * (1/10^6) = 0.095000005$$

$$P(\text{kyoto}) = 0.95 * 0.00 + 0.05 * (1/10^6) = 0.000000005$$

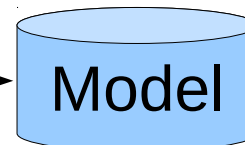
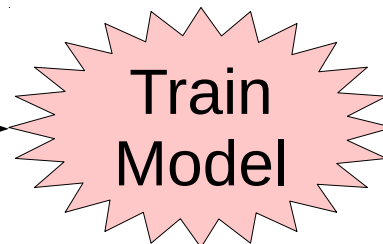
Evaluating Language Models

Experimental Setup

- Use training and test sets

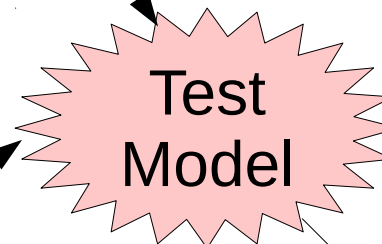
Training Data

i live in osaka
i am a graduate student
my school is in nara
...



Testing Data

i live in nara
i am a student
i have lots of homework
...



Model Accuracy

Likelihood
Log Likelihood
Entropy
Perplexity

Likelihood

- Likelihood is the **probability of some observed data** (the test set W_{test}), given the model M

$$P(W_{test} | M) = \prod_{w \in W_{test}} P(w | M)$$

i live in nara

i am a student

my classes are hard

$$P(w="i live in nara"|M) = 2.52 \cdot 10^{-21}$$

X

$$P(w="i am a student"|M) = 3.48 \cdot 10^{-19}$$

X

$$P(w="my classes are hard"|M) = 2.15 \cdot 10^{-34}$$

=

$$1.89 \cdot 10^{-73}$$

Log Likelihood

- Likelihood uses **very small numbers**=underflow
- Taking the log resolves this problem

$$\log P(W_{test}|M) = \sum_{w \in W_{test}} \log P(w|M)$$

i live in nara

i am a student

my classes are hard

$$\begin{aligned} \log P(w="i live in nara"|M) &= & -20.58 \\ &+ \\ \log P(w="i am a student"|M) &= & -18.45 \\ &+ \\ \log P(w="my classes are hard"|M) &= & -33.67 \\ &= & -72.60 \end{aligned}$$

Calculating Logs

- Python's math package has a function for logs

```
import math
```

```
print(math.log(100))          # ln(100)  
print(math.log(100, 10))     # log10(100)
```

```
$ ./my-program.py  
4.60517018599  
2.0
```

Entropy

- Entropy H is average negative \log_2 likelihood per word

$$H(W_{test} | M) = \frac{1}{|W_{test}|} \sum_{w \in W_{test}} -\log_2 P(w | M)$$

i live in nara i am a student my classes are hard	$\log_2 P(w="i live in nara" M)=$	(68.43 + 61.32 + 111.84)
	$\log_2 P(w="i am a student" M)=$	/ # of words= 12
	$\log_2 P(w="my classes are hard" M)=$	= 20.13

* note, we can also count $\langle /s \rangle$ in # of words (in which case it is 15)²⁰

Perplexity

- Equal to two to the power of per-word entropy

$$PPL = 2^H$$

- (Mainly because it makes more impressive numbers)
- For uniform distributions, equal to the size of vocabulary

$$V = 5 \quad H = -\log_2 \frac{1}{5} \quad PPL = 2^H = 2^{-\log_2 \frac{1}{5}} = 2^{\log_2 5} = 5$$

Coverage

- The percentage of known words in the corpus

a bird a cat a dog a </s>

“dog” is an unknown word

Coverage: $7/8$ *

* often omit the sentence-final symbol → $6/7$

Exercise

Exercise

- Write two programs
 - train-unigram: Creates a unigram model
 - test-unigram: Reads a unigram model and calculates entropy and coverage for the test set
- Test them test/01-train-input.txt test/01-test-input.txt
- Train the model on data/wiki-en-train.word
- Calculate entropy and coverage on data/wiki-en-test.word
- Report your scores next week

train-unigram Pseudo-Code

create a **map** *counts*

create a **variable** *total_count* = 0

for each *line* **in** the *training_file*

split *line* into an array of *words*

append “</s>” to the end of *words*

for each *word* **in** *words*

add 1 to *counts[word]*

add 1 to *total_count*

open the *model_file* for writing

for each *word, count* **in** *counts*

probability = *counts[word]/total_count*

print *word, probability* **to** *model_file*

test-unigram Pseudo-Code

$$\lambda_1 = 0.95, \lambda_{\text{unk}} = 1 - \lambda_1, V = 1000000, W = 0, H = 0$$

Load Model

create a **map** *probabilities*
for each line in *model_file*
split *line* into *w* and *P*
set *probabilities*[*w*] = *P*

Test and Print

for each line in *test_file*
split *line* into an array of *words*
append “</s>” to the end of *words*
for each w in *words*
add 1 to *W*
set $P = \lambda_{\text{unk}} / V$
if *probabilities*[*w*] exists
set $P += \lambda_1 * \text{probabilities}[w]$
else
add 1 to *unk*
add $-\log_2 P$ to *H*

print “entropy = ” + H/W
print “coverage = ” + $(W - \text{unk})/W$

Thank You!