

# Lattice and Hypergraph MERT

Graham Neubig

Nara Institute of Science and Technology (NAIST)

12/20/2012

# Papers Introduced:

- “Lattice-based Minimum Error Rate Training for Statistical Machine Translation”

Wolfgang Macherey, Franz Josef Och, Ignacio Thayer,  
Jakob Uszkoreit (Google)  
EMNLP 2008

- “Efficient Minimum Error Rate Training and Minimum Bayes-Risk Decoding for Translation Hypergraphs and Lattices”

Shankar Kumar, Wolfgang Macherey, Chris Dyer, Franz  
Och (Google/University of Maryland)  
ACL-IJCNLP 2009

# Summary

- Minimum error rate training (MERT) is used to train the parameters for machine translation
- Normal MERT uses n-best lists
- However, there is not enough diversity in n-best lists,  
→ unstable training & large accuracy fluctuations
- As a solution these papers perform MERT over
  - lattices for phrase-based translation [Macherey+ 08]
  - hypergraphs for tree-based translation [Kumar+ 09]
- This leads to more stable training in fewer iterations

# Tuning/MERT

# Tuning

- Scores of translation, reordering, and language models

	LM	TM	RM	
○ Taro visited Hanako	-4	-3	-1	-8
✗ the Taro visited the Hanako	-5	-4	-1	-10
✗ Hanako visited Taro	-2	-3	-2	-7 → Best Score ✗

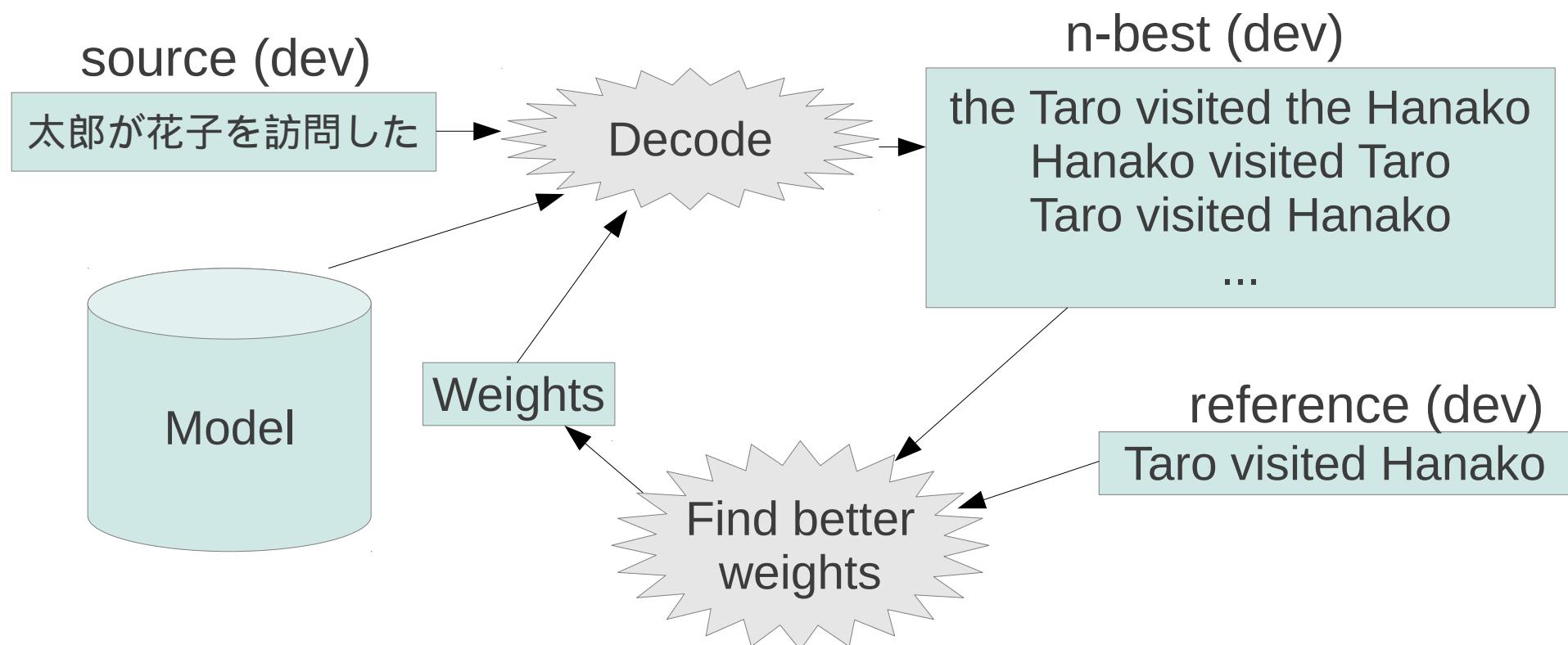
- If we add weights, we can get better answers:

	LM	TM	RM	Best Score
○ Taro visited Hanako	0.2*-4	0.3*-3	0.5*-1	→ ○ -2.2
✗ the Taro visited the Hanako	0.2*-5	0.3*-4	0.5*-1	-2.7
✗ Hanako visited Taro	0.2*-2	0.3*-3	0.5*-2	-2.3

- Tuning finds these weights:  $w_{LM} = 0.2$   $w_{TM} = 0.3$   $w_{RM} = 0.5$

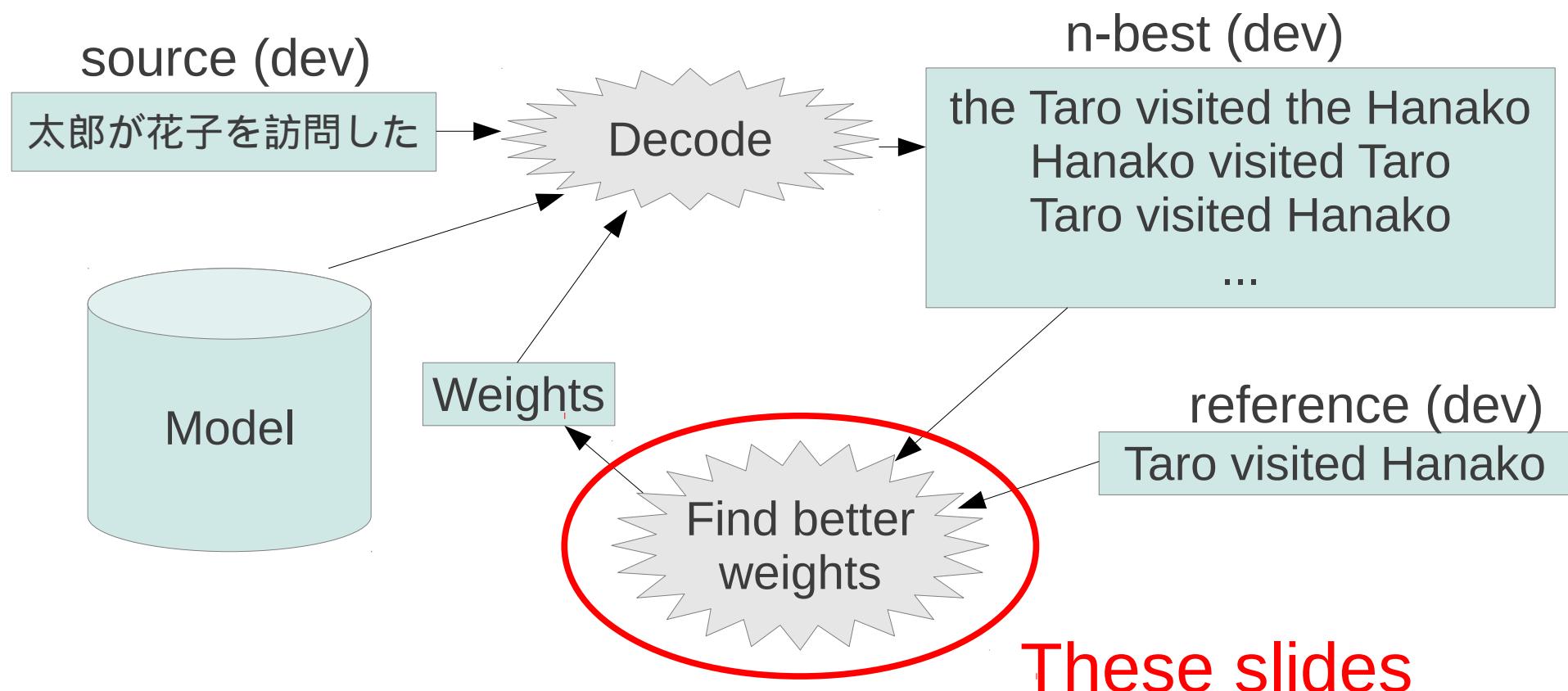
# MERT

- MERT performs iterations to increase the score  
[Och 03]



# MERT

- MERT performs iterations to increase the score  
[Och 03]



# MERT Weight Update:

- Adjust one weight at a time

	<u>Weights</u>			<u>Score</u>
	$w_{LM}$	$w_{TM}$	$w_{RM}$	
Initial:	0.1	0.1	0.1	0.20
Optimize $w_{LM}$ :	0.4	0.1	0.1	0.32
Optimize $w_{TM}$ :	0.4	0.1	0.1	0.32
Optimize $w_{RM}$ :	0.4	0.1	0.3	0.4
Optimize $w_{LM}$ :	0.35	0.1	0.3	0.41
Optimize $w_{TM}$ :				

# Updating One Weight:

- We start with:  
n-best list

$f_1$	$\phi_{LM}$	$\phi_{TM}$	$\phi_{RM}$	BLEU*
$e_{1,1}$	1	0	-1	0
$e_{1,2}$	0	1	0	1
$e_{1,3}$	1	0	1	0

$f_2$	$\phi_{LM}$	$\phi_{TM}$	$\phi_{RM}$	BLEU*
$e_{2,1}$	1	0	-2	0
$e_{2,2}$	3	0	1	0
$e_{2,3}$	2	1	2	1

fixed weights:

$$w_{LM} = -1, w_{TM} = 1$$

weight to be adjusted:

$$w_{RM} = ???$$

---

\* Calculating BLEU for one sentence is a bit simplified, usually we compute for the whole corpus

# Updating One Weight:

- Next, transform each hypothesis into lines:

$$y = \color{blue}{a} \color{green}{x} + \color{red}{b}$$

- Where:
  - $a$  is the value of the feature to be adjusted
  - $b$  is the weighted sum of the fixed features
  - $x$  is the weight to be adjusted (unknown)

# Updating One Weight:

- Example:

$w_{LM} = -1, w_{TM} = 1, w_{RM} = ???$

$$y = a x + b$$

$$a = \phi_{RM} \quad b = w_{LM} \phi_{LM} + w_{TM} \phi_{TM}$$

$f_1$	$\phi_{LM}$	$\phi_{TM}$	$\phi_{RM}$
$e_{1,1}$	1	0	-1
$e_{1,2}$	0	1	0
$e_{1,3}$	1	0	1

$$a_{1,1} = -1$$

$$b_{1,1} = -1$$

$$a_{1,2} = 0$$

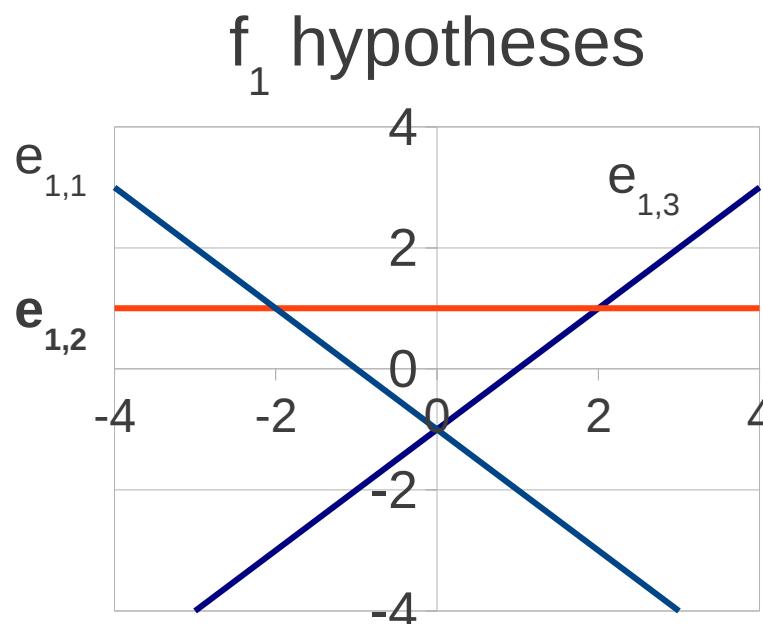
$$b_{1,2} = 1$$

$$a_{1,3} = 1$$

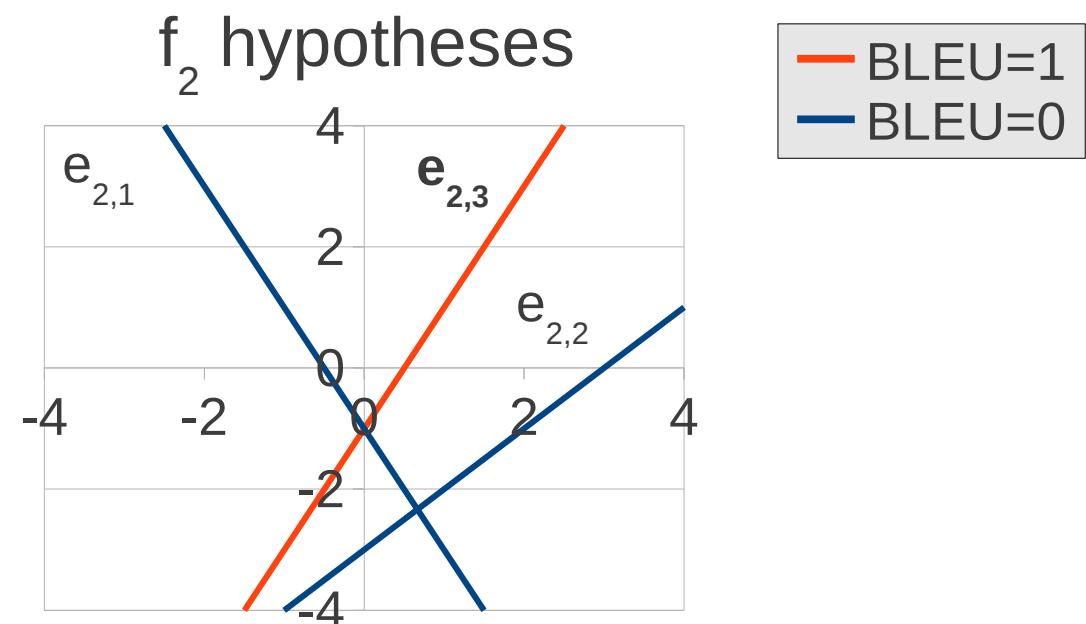
$$b_{1,3} = -1$$

# Updating One Weight:

- Draw lines on a graph:  $y = a x + b$



$$\begin{array}{ll} a_{1,1} = -1 & b_{1,1} = -1 \\ a_{1,2} = 0 & b_{1,2} = 1 \\ a_{1,3} = 1 & b_{1,3} = -1 \end{array}$$

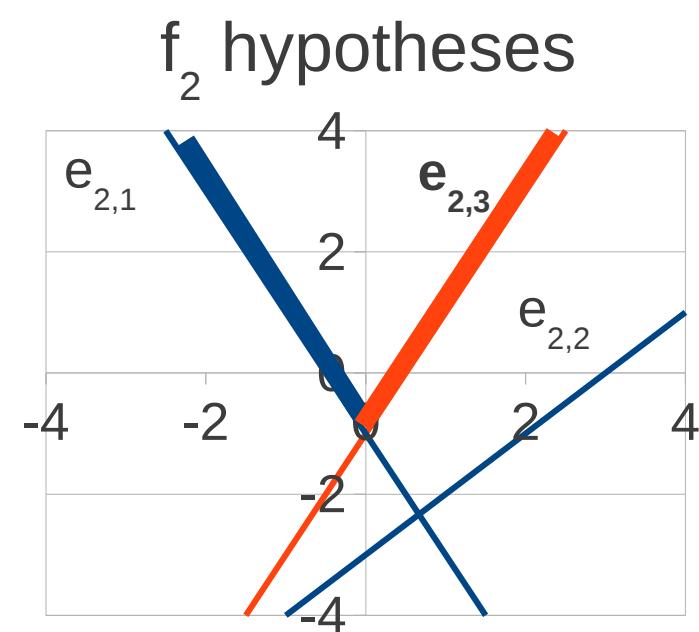
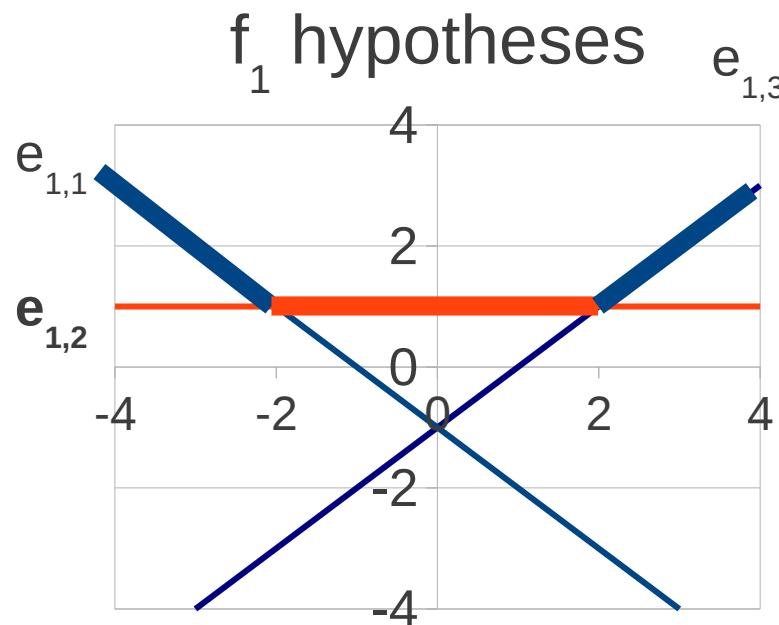


BLEU=1  
BLEU=0

$$\begin{array}{ll} a_{2,1} = -2 & b_{2,1} = -1 \\ a_{2,2} = 1 & b_{2,2} = -3 \\ a_{2,3} = -2 & b_{2,3} = 1 \end{array}$$

# Updating One Weight:

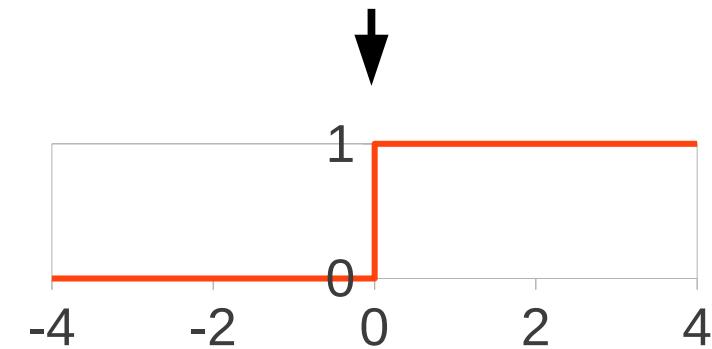
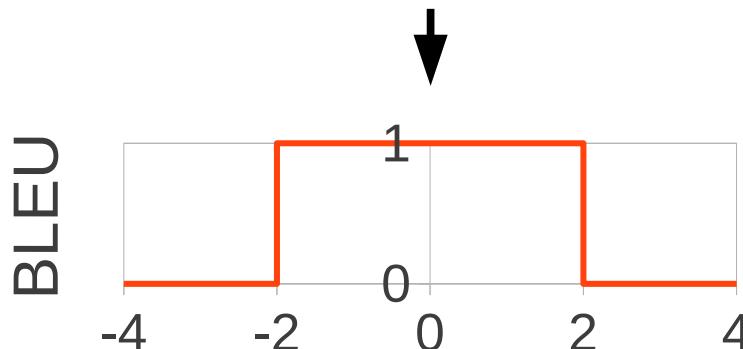
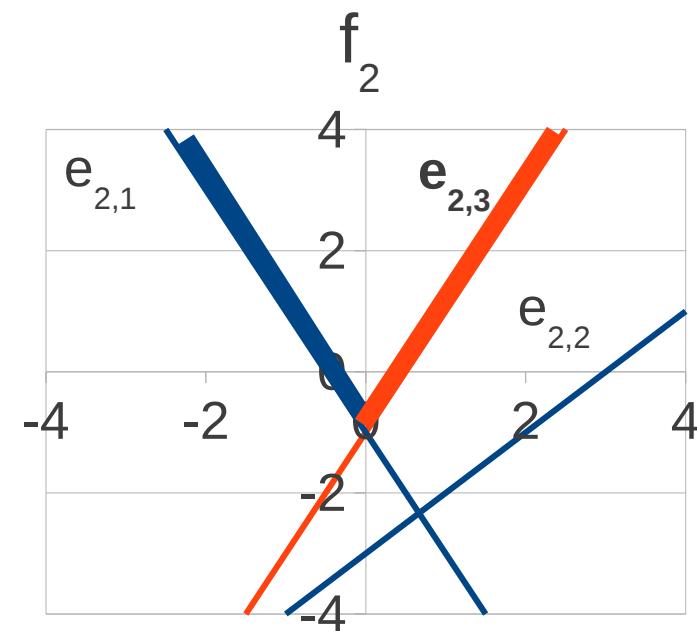
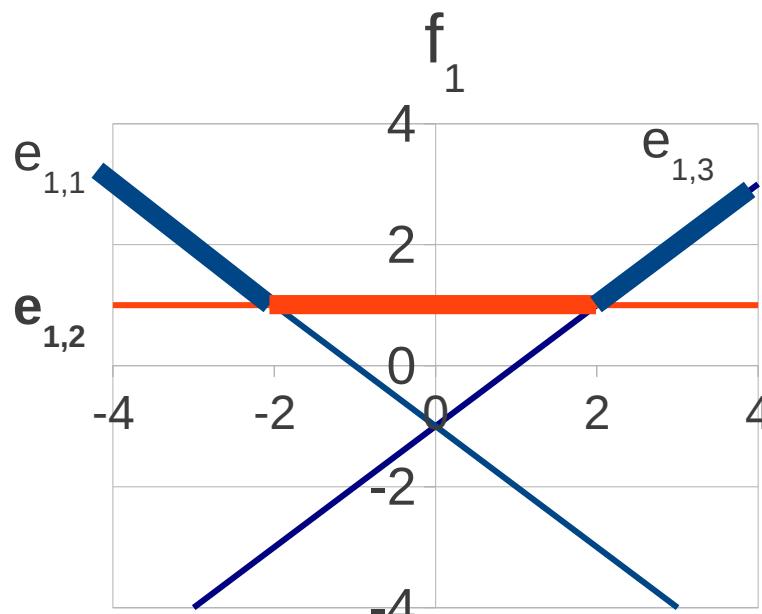
- Find the lines that are highest for each range of  $x$ :



- This is called the **convex hull** (or upper envelope)

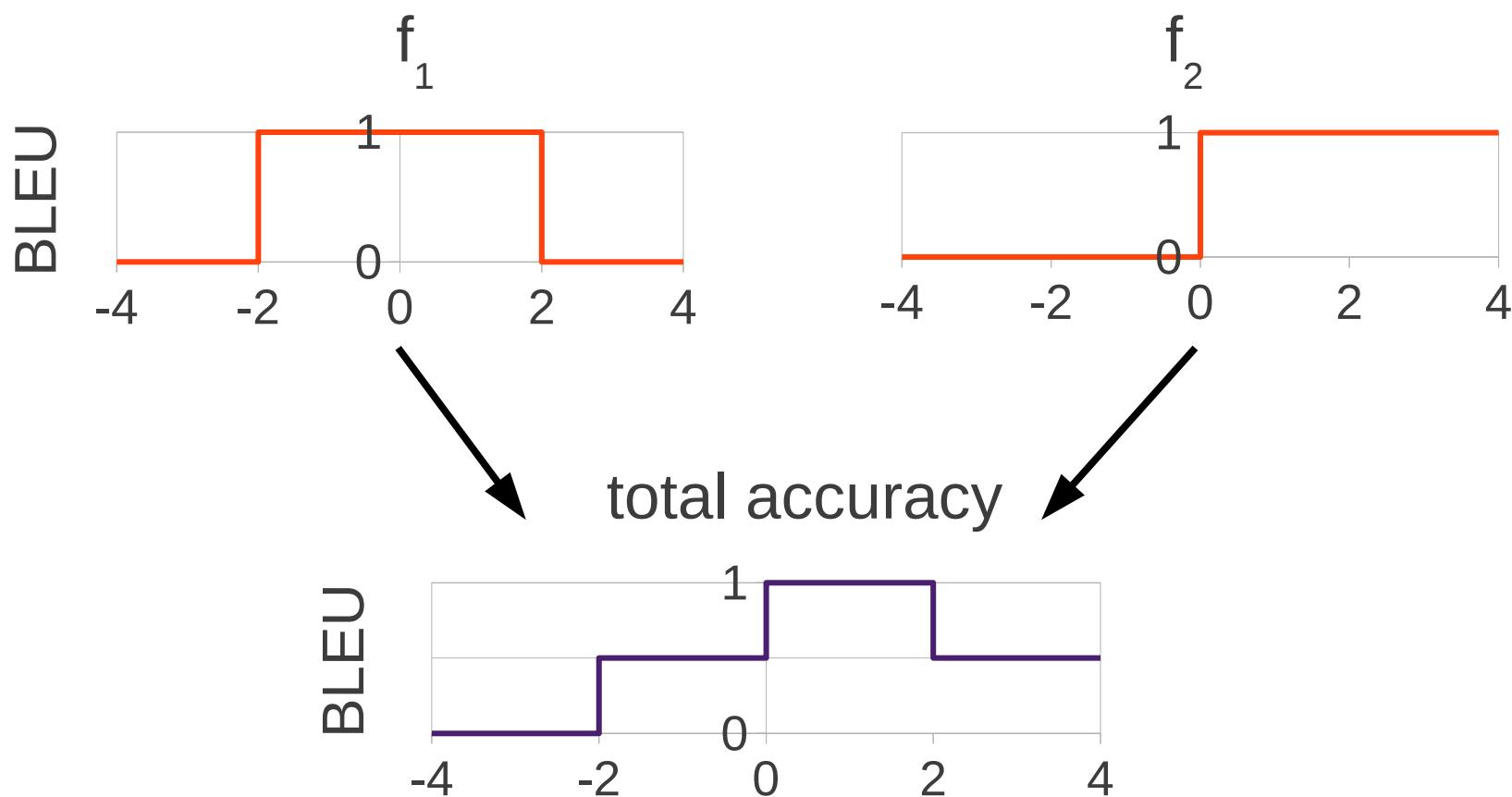
# Updating One Weight:

- Using the convex hull, find scores at each range:



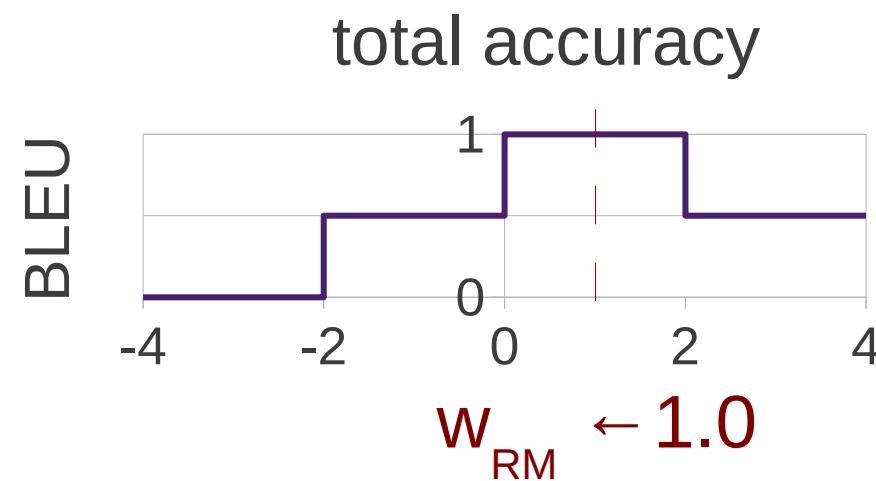
# Updating One Weight:

- Combine multiple sentences into a single error plane:



# Updating One Weight:

- Choose middle of best region:



# Summary

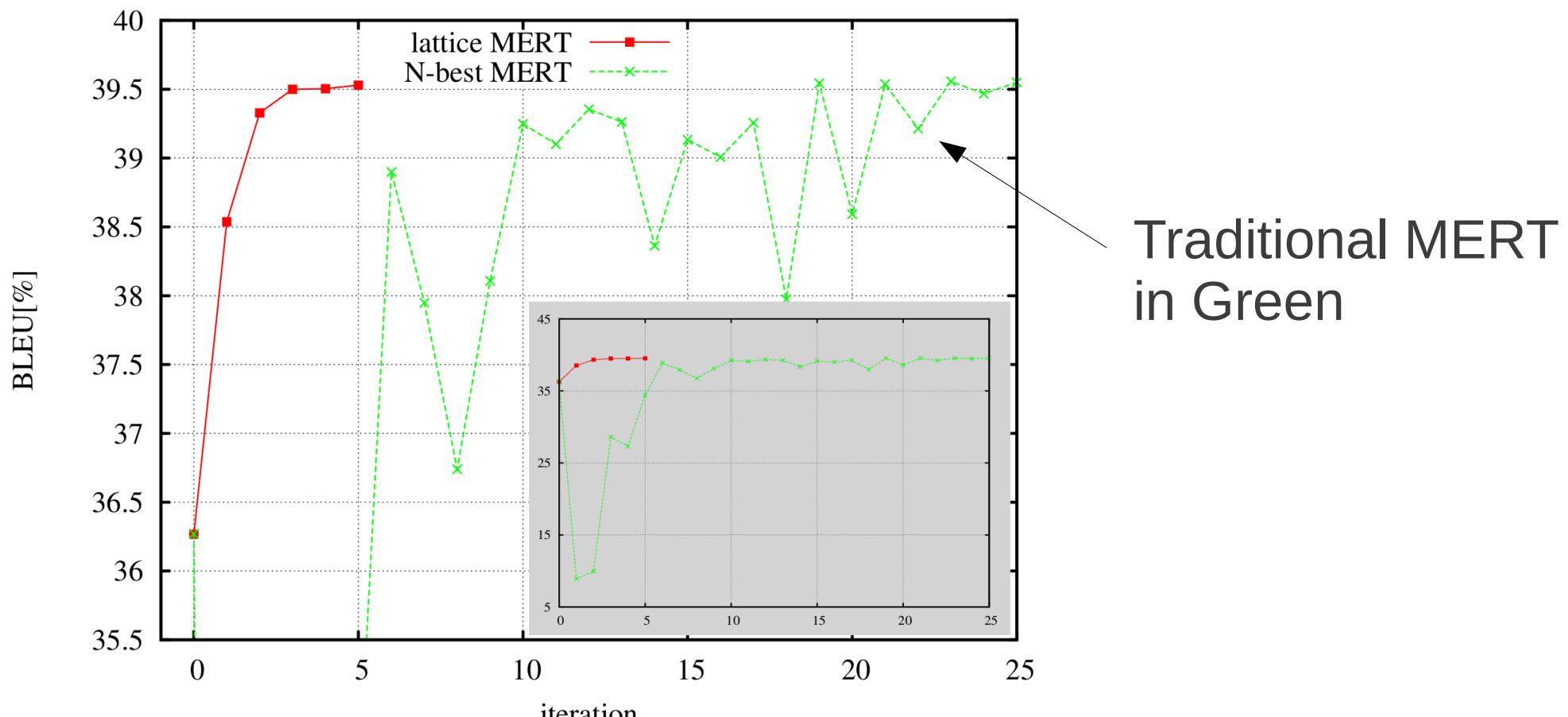
- For each sentence:
  - Create lines for each n-best hypothesis
  - Combine lines and find upper envelope
  - Transform upper envelope into error surface
- Combine error surfaces into one
- Find the range with the highest score
- Set the weight to the middle of the range

# Summary

- For each sentence: **Problem!** (not enough diversity)
  - Create lines for each **n-best** hypothesis
  - Combine lines and find upper envelope
  - Transform upper envelope into error surface
- Combine error surfaces into one
- Find the range with the highest score
- Set the weight to the middle of the range

# Result of Lack of Diversity

- Unstable training:

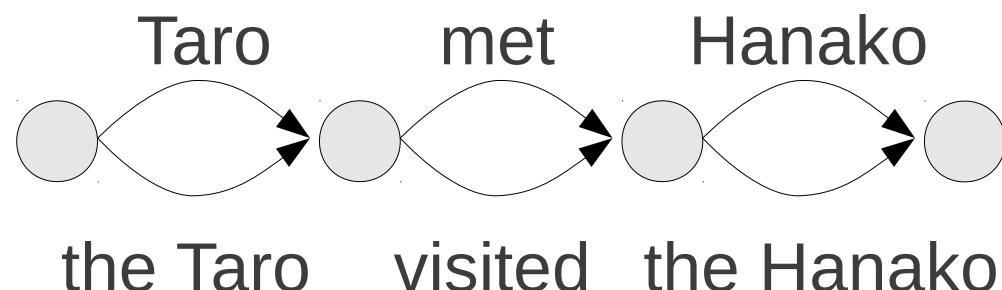


[Macherey 08]

# Lattice MERT

# Translation Lattice

- Represent many hypotheses compactly:

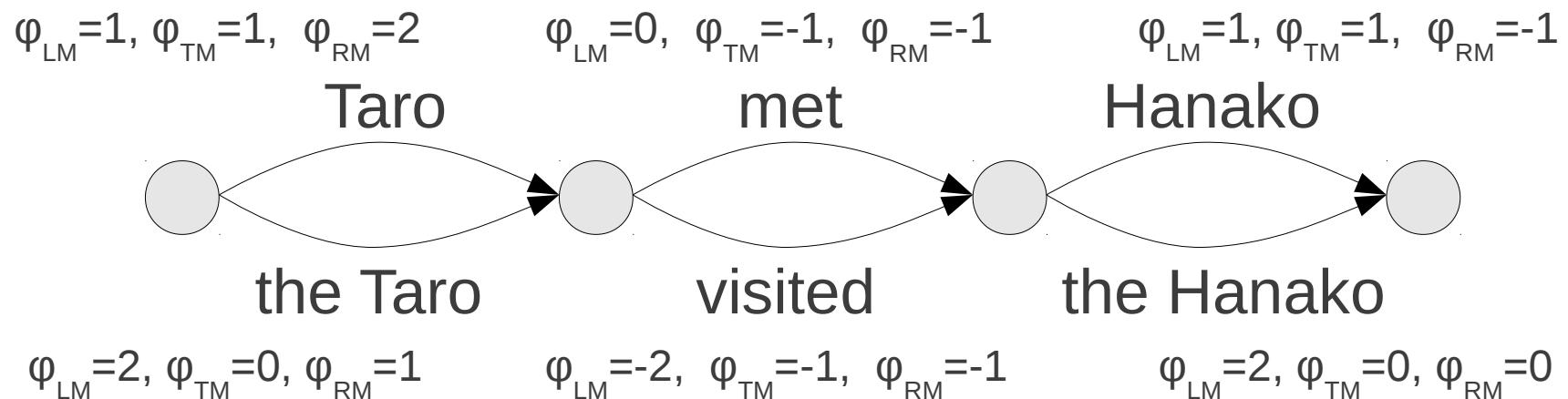


**8 hypotheses  
in only  
6 edges**

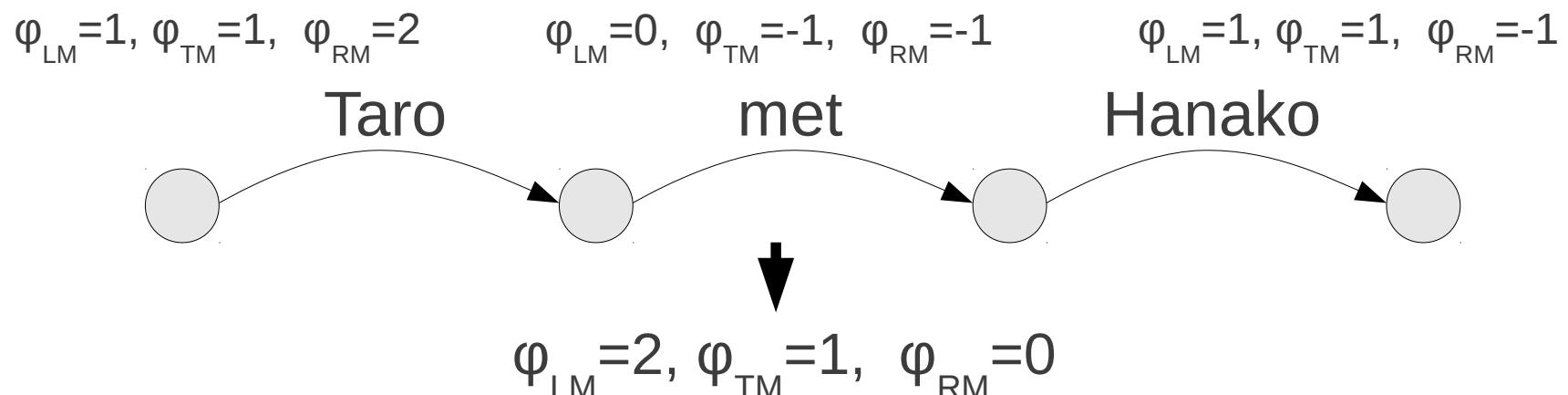
- MERT on lattices can solve the diversity problem

# Factoring Feature Functions

- Each edge in the lattice has a feature value:



- Hypothesis's features are sum of edge features:



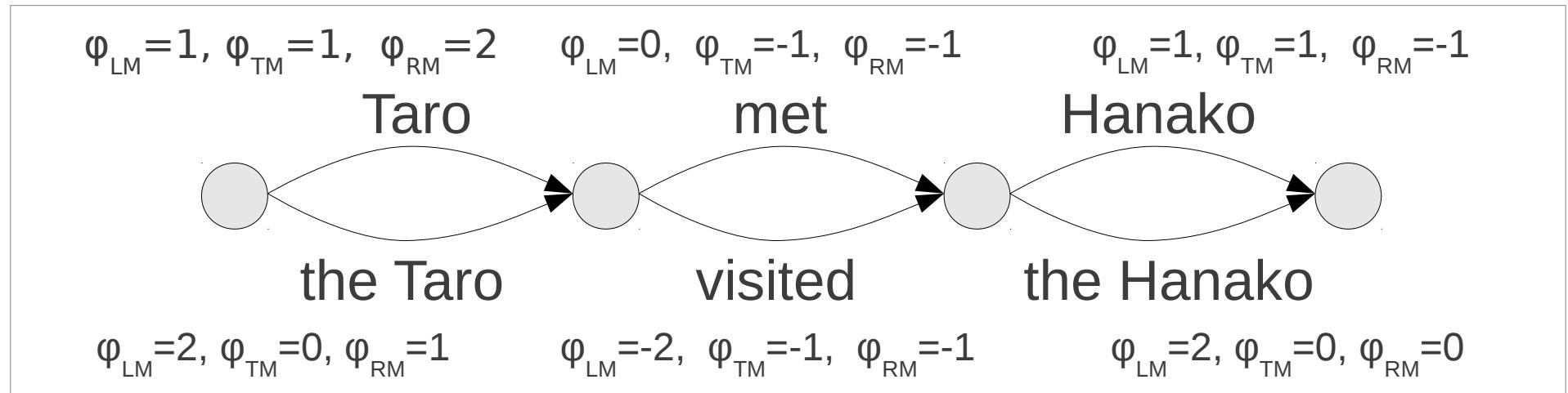
# MERT on Lattices:

- For each sentence:  
  - Transform each edge into lines
  - Find the upper envelope for the lattice
  - Transform upper envelope into error surface
  - Combine error surfaces into one
  - Find the range with the highest score
  - Set the weight to the middle of the range

**Only different part!!**

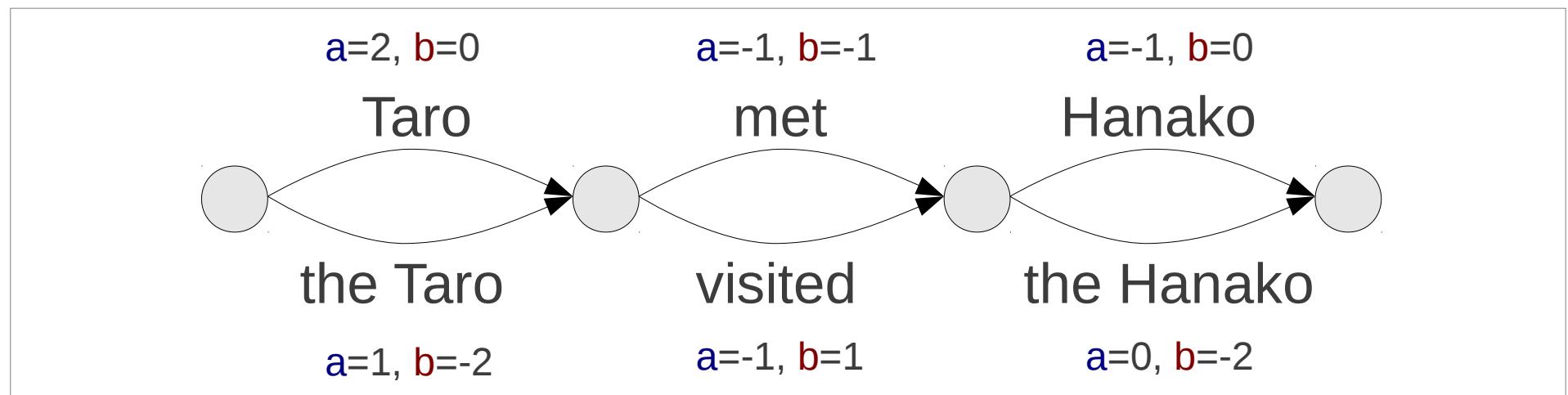


# First, Transform each Edge into Lines



$$w_{LM} = -1, w_{TM} = 1, w_{RM} = ??? \quad \downarrow \quad y = a x + b$$

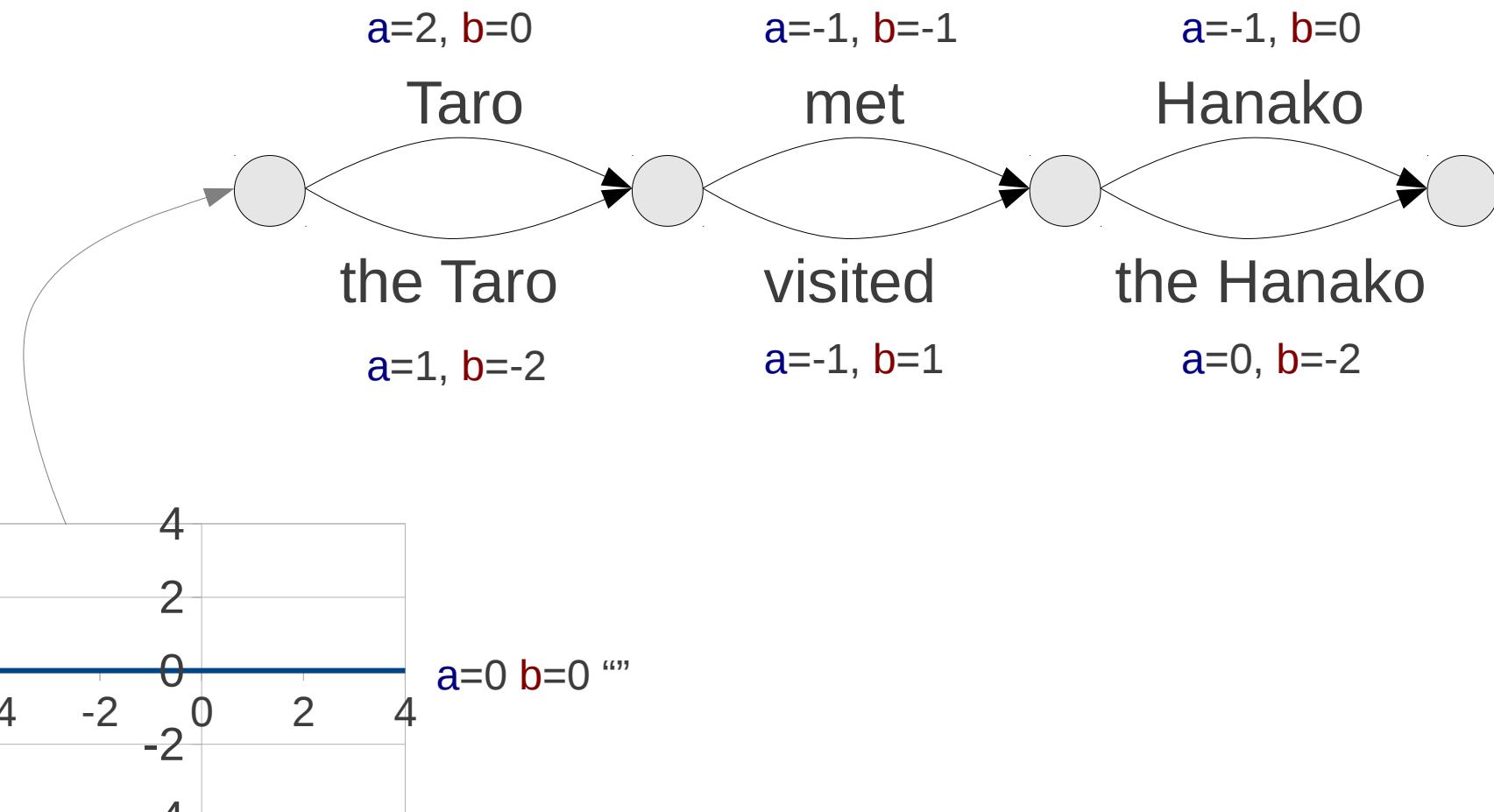
$$a = \varphi_{RM} \quad b = w_{LM} \varphi_{LM} + w_{TM} \varphi_{TM}$$



# Finding the Upper Envelope for Lattices:

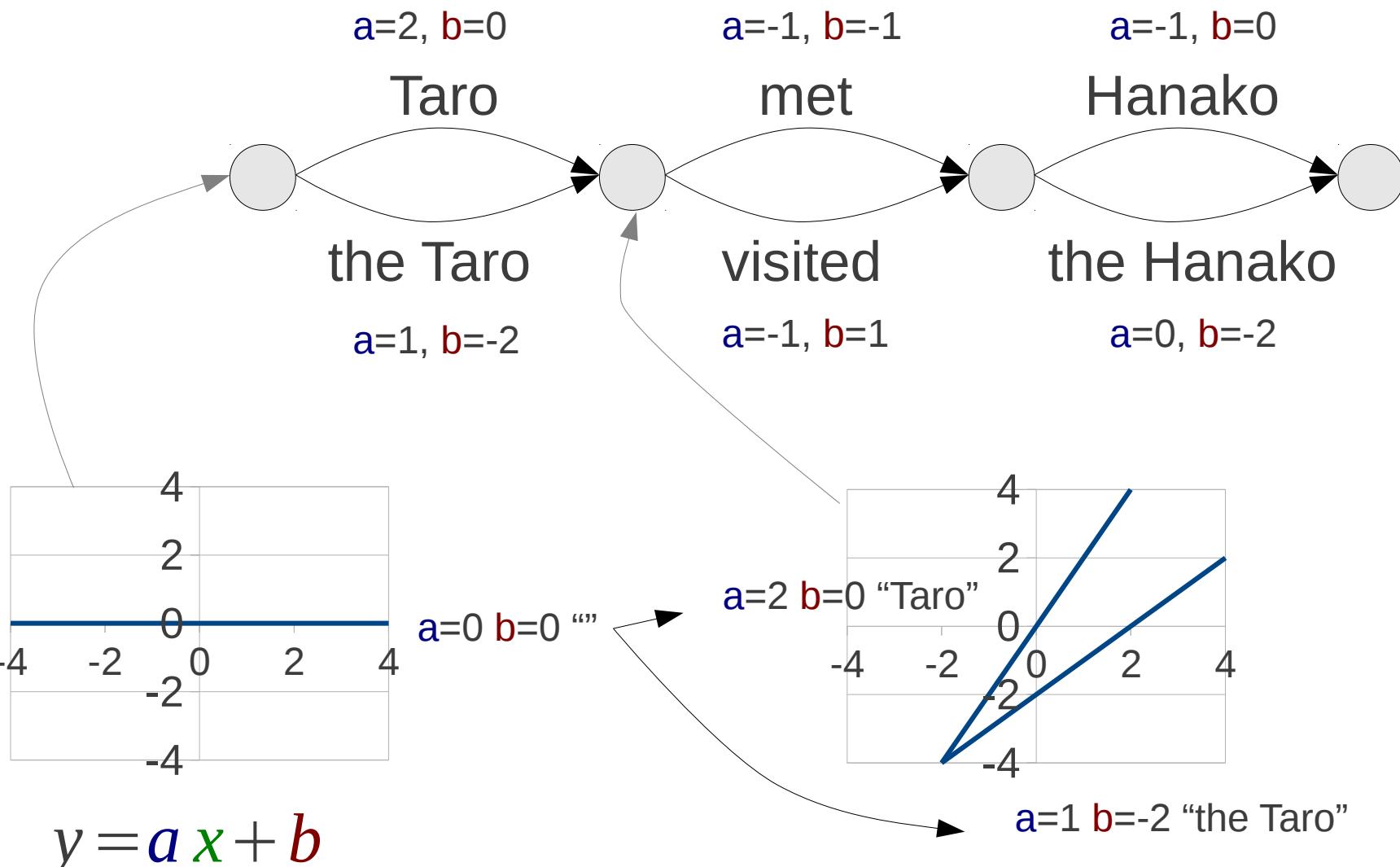
- Can be done with dynamic programming
- 1) Start with flat envelope for initial node
- 2) Calculate upper envelope for next node using previous nodes

# Start with Flat Envelope

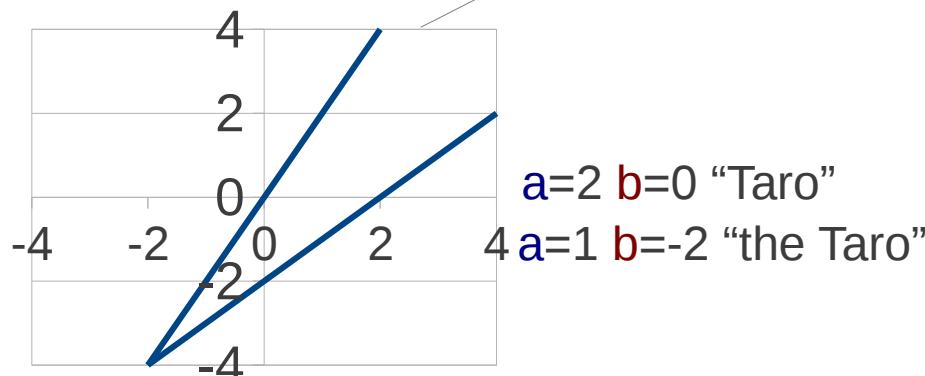
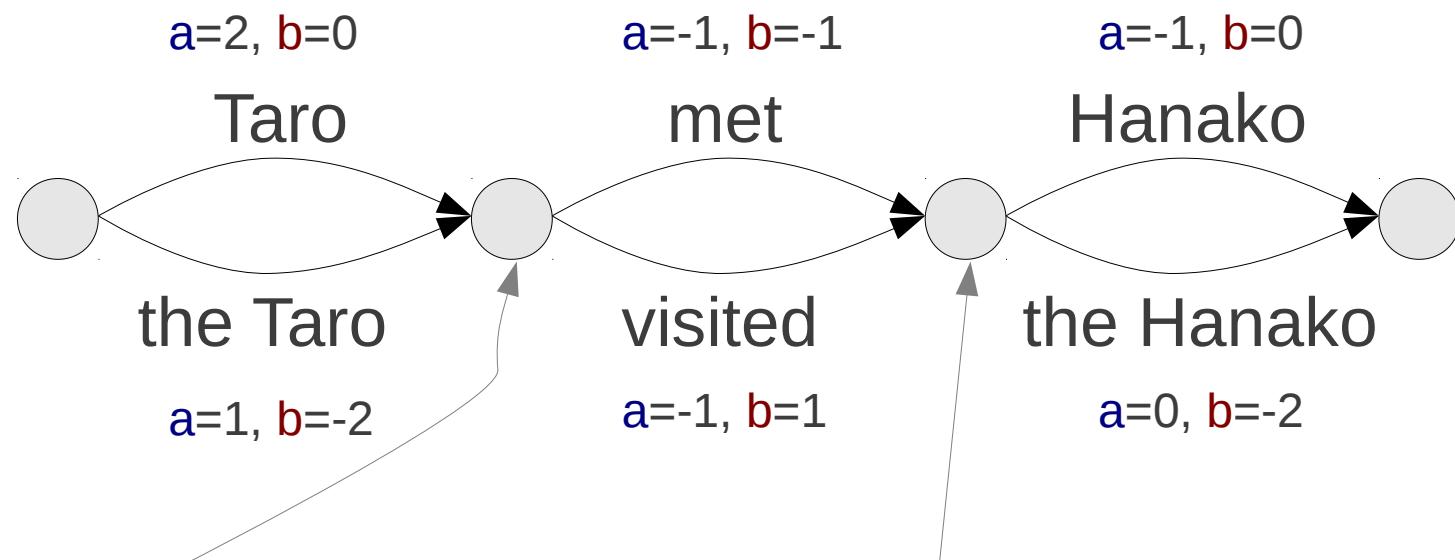


$$y = a \textcolor{green}{x} + b$$

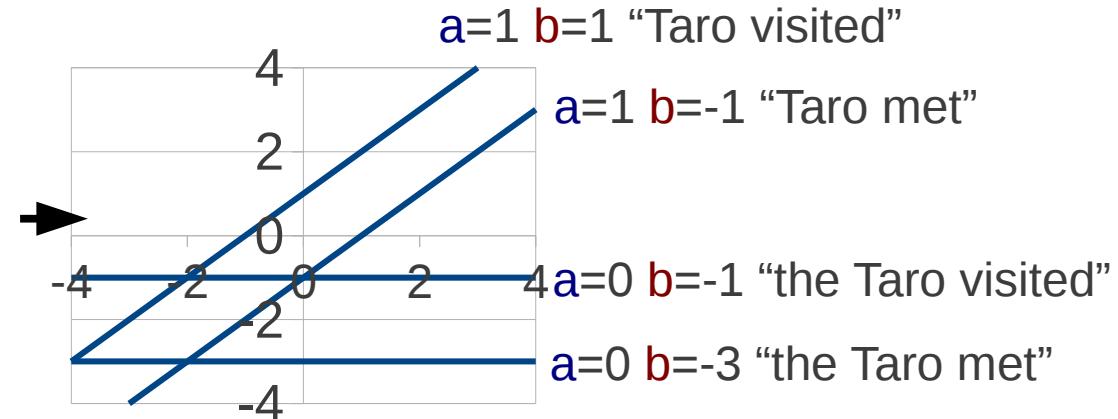
# Add First Node



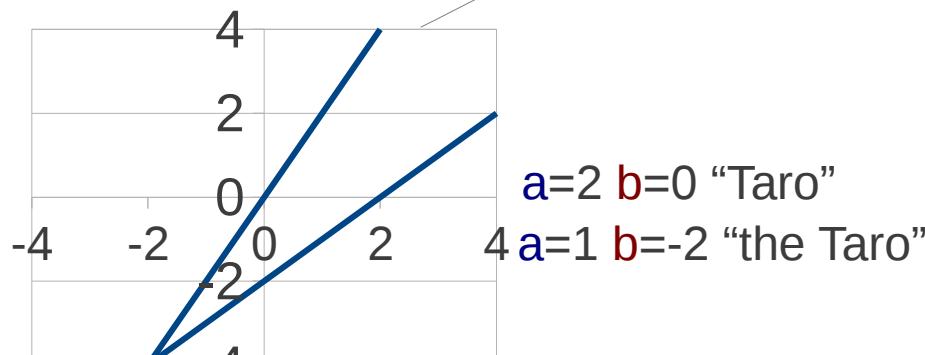
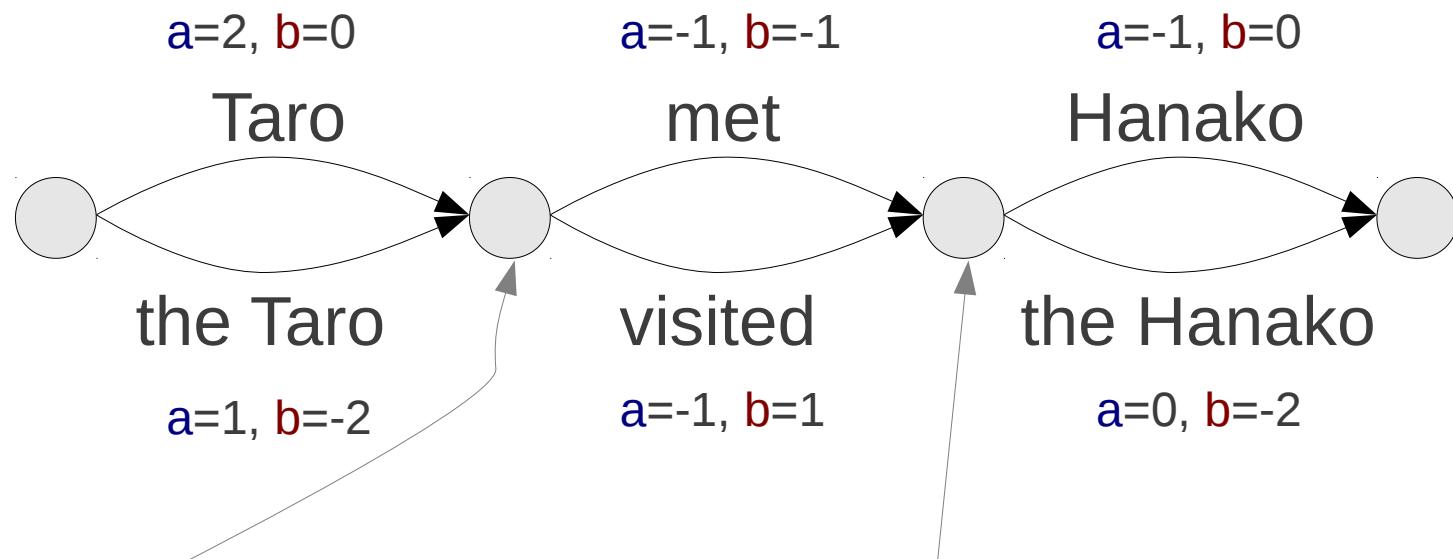
# Add Second



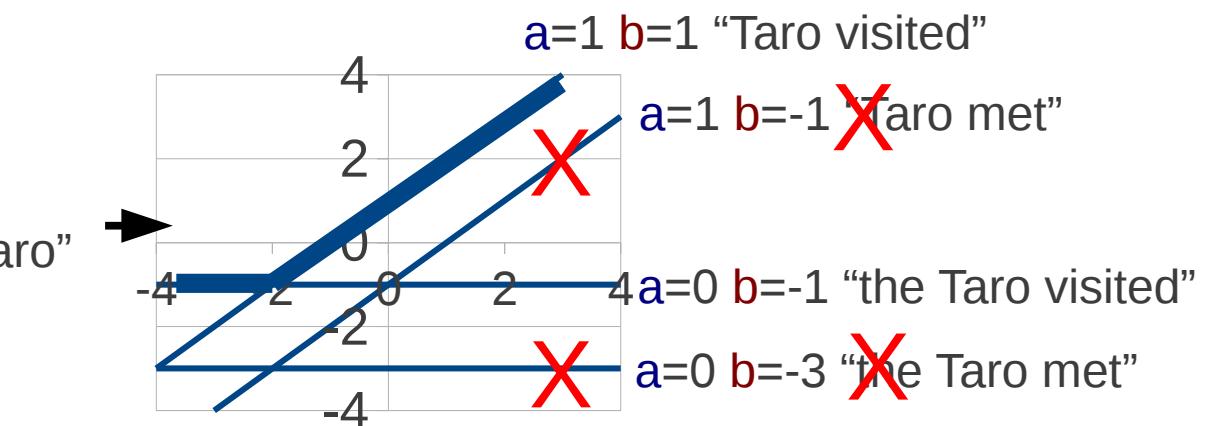
$$y = a x + b$$



# Add Second

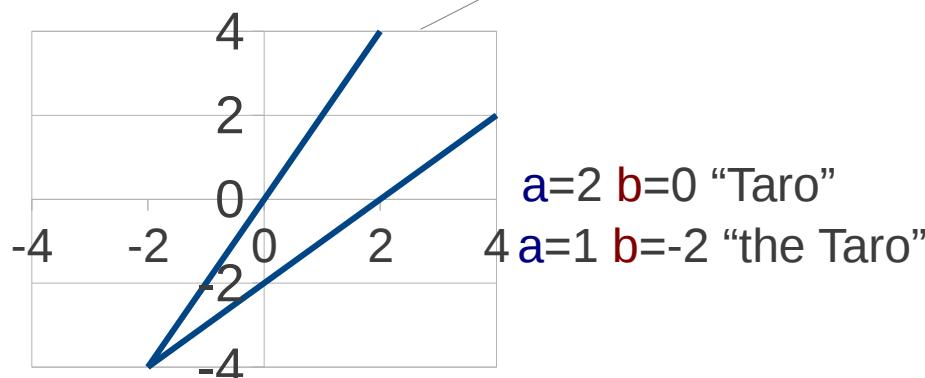
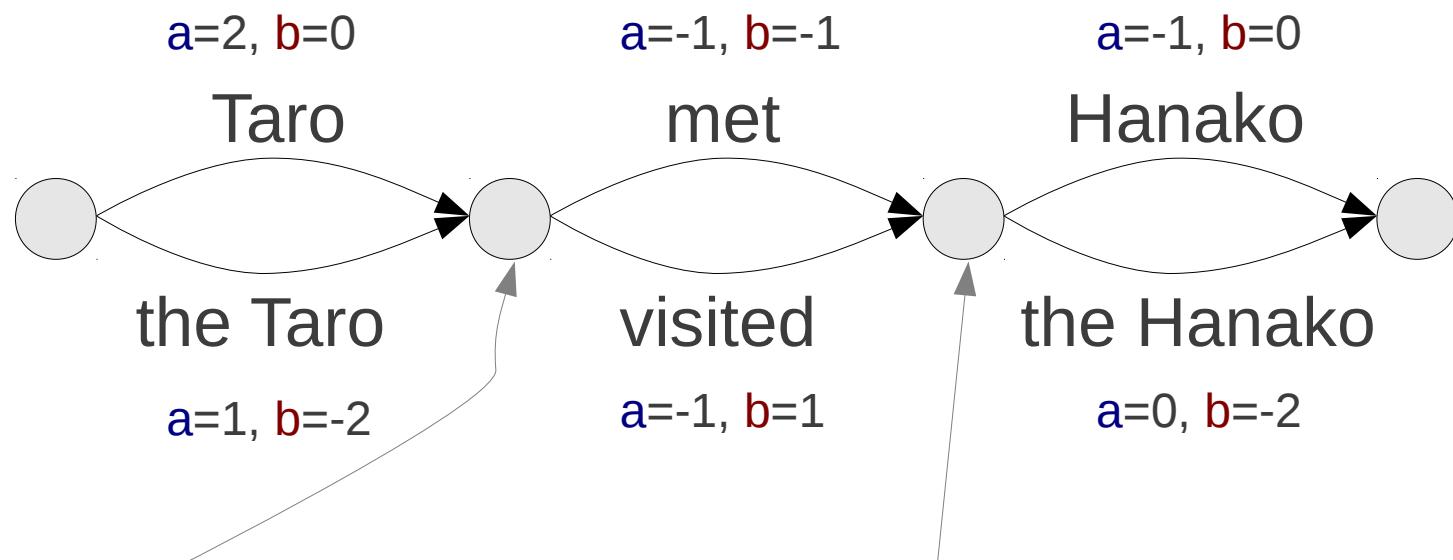


$$y = a x + b$$

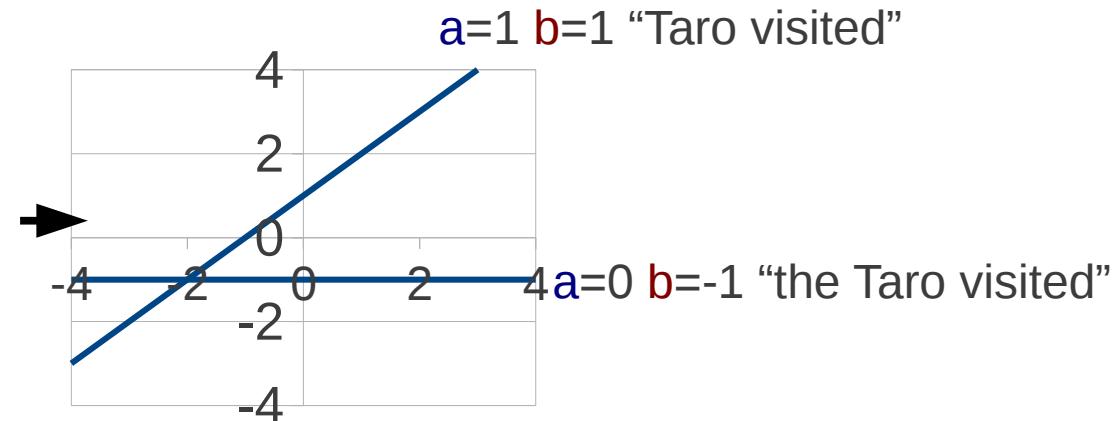


Delete all lines not in upper envelope

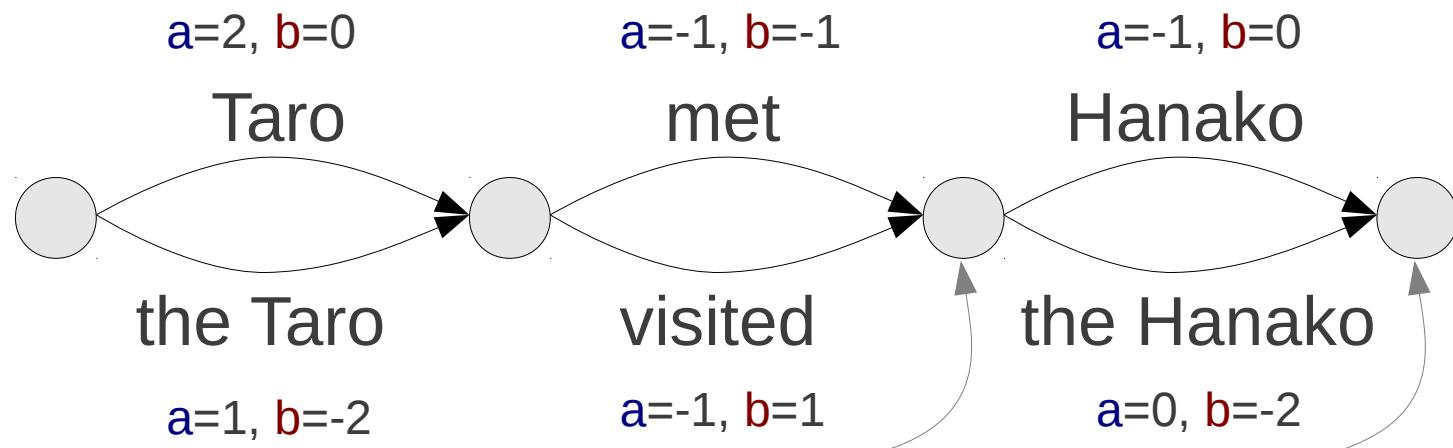
# Add Second



$$y = a x + b$$

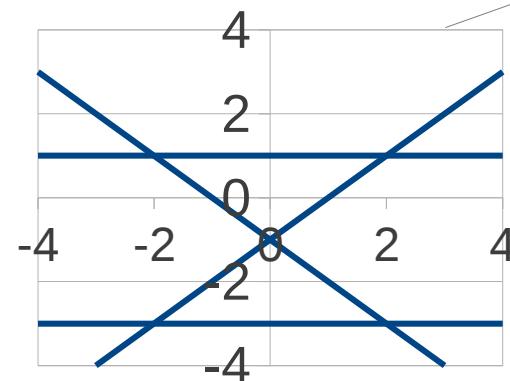
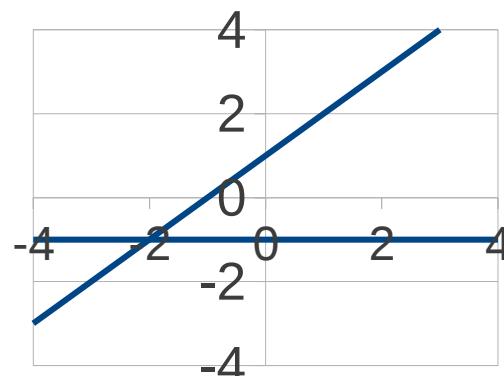


# Add Third



$a=1 \ b=1$  "Taro visited"

$a=0 \ b=-1$  "the Taro visited"



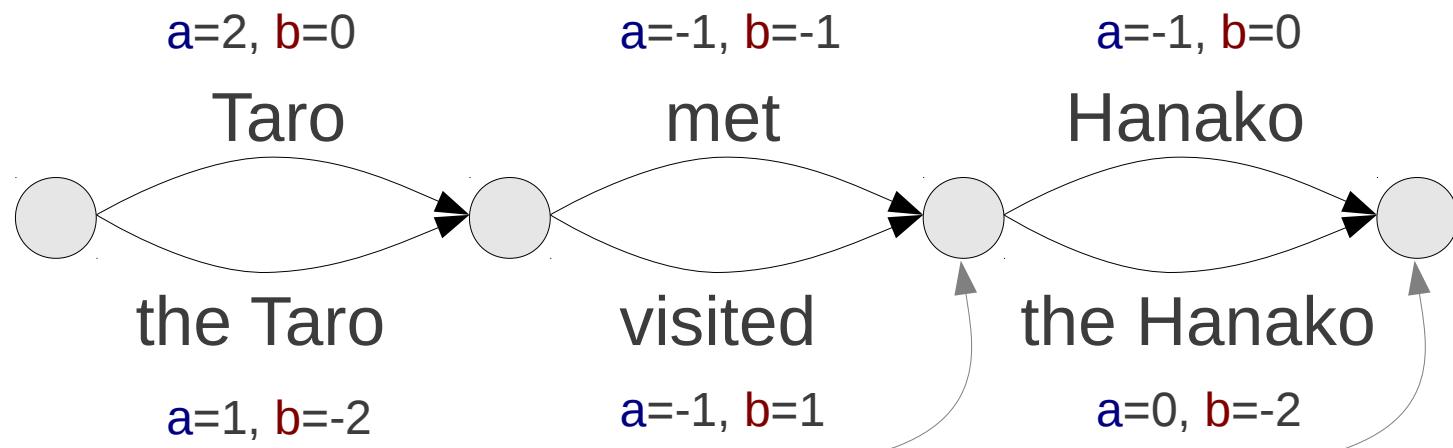
$a=1 \ b=-1$  "Taro visited the Hanako"

$a=0 \ b=1$  "Taro visited Hanako"

$a=0 \ b=-3$  "the Taro visited the Hanako"

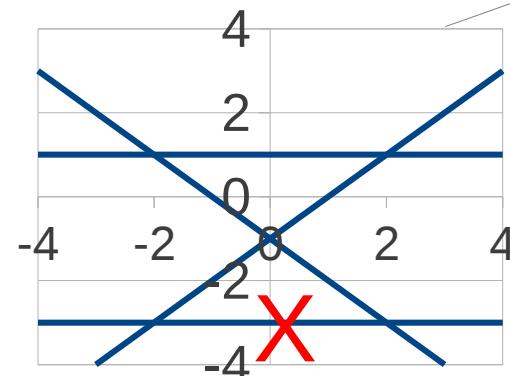
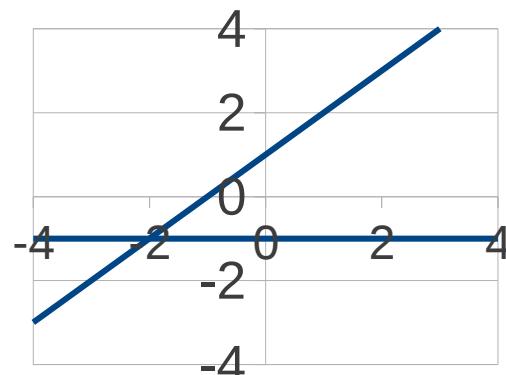
$a=-1 \ b=-1$  "the Taro visited Hanako"

# Add Third



$a=1 \ b=1$  "Taro visited"

$a=0 \ b=-1$  "the Taro visited"



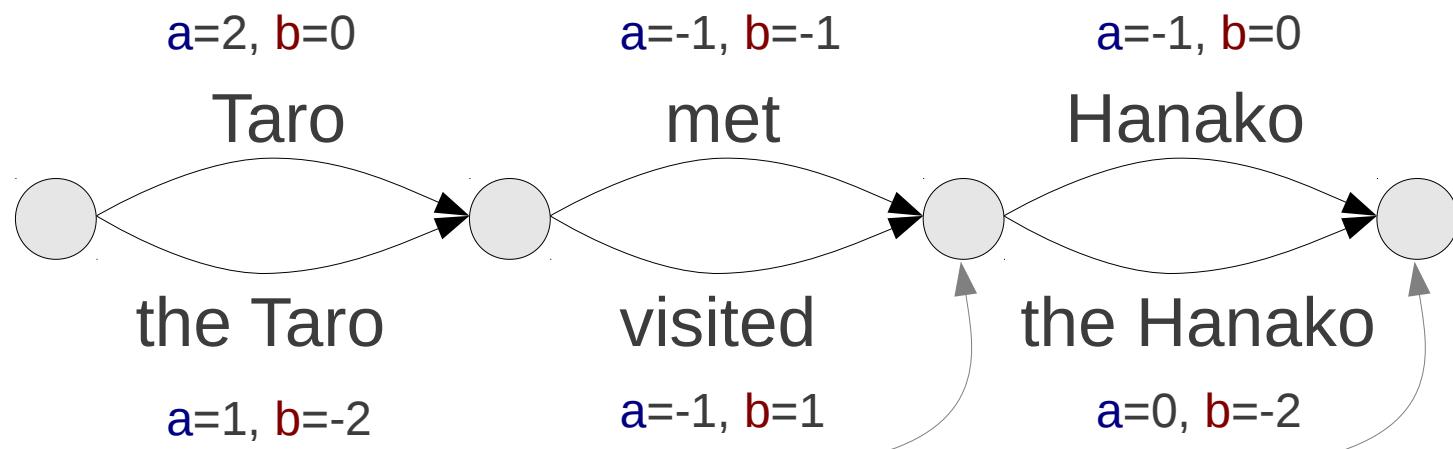
$a=1 \ b=-1$  "Taro visited the Hanako"

$a=0 \ b=1$  "Taro visited Hanako"

$a=0 \ b=-3$  "the Taro visited the Hanako" X

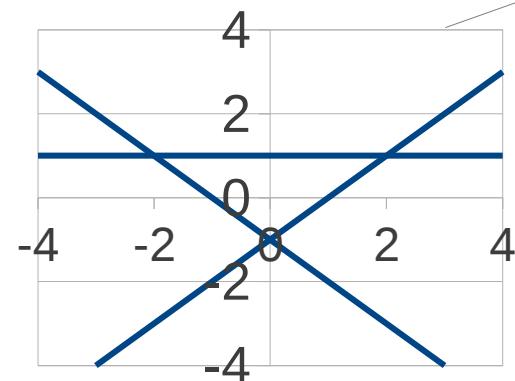
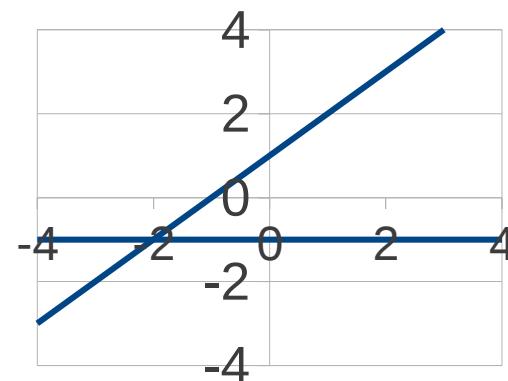
$a=-1 \ b=-1$  "the Taro visited Hanako"

# Add Third



$a=1 \ b=1$  "Taro visited"

$a=0 \ b=-1$  "the Taro visited"



$$y = a x + b$$

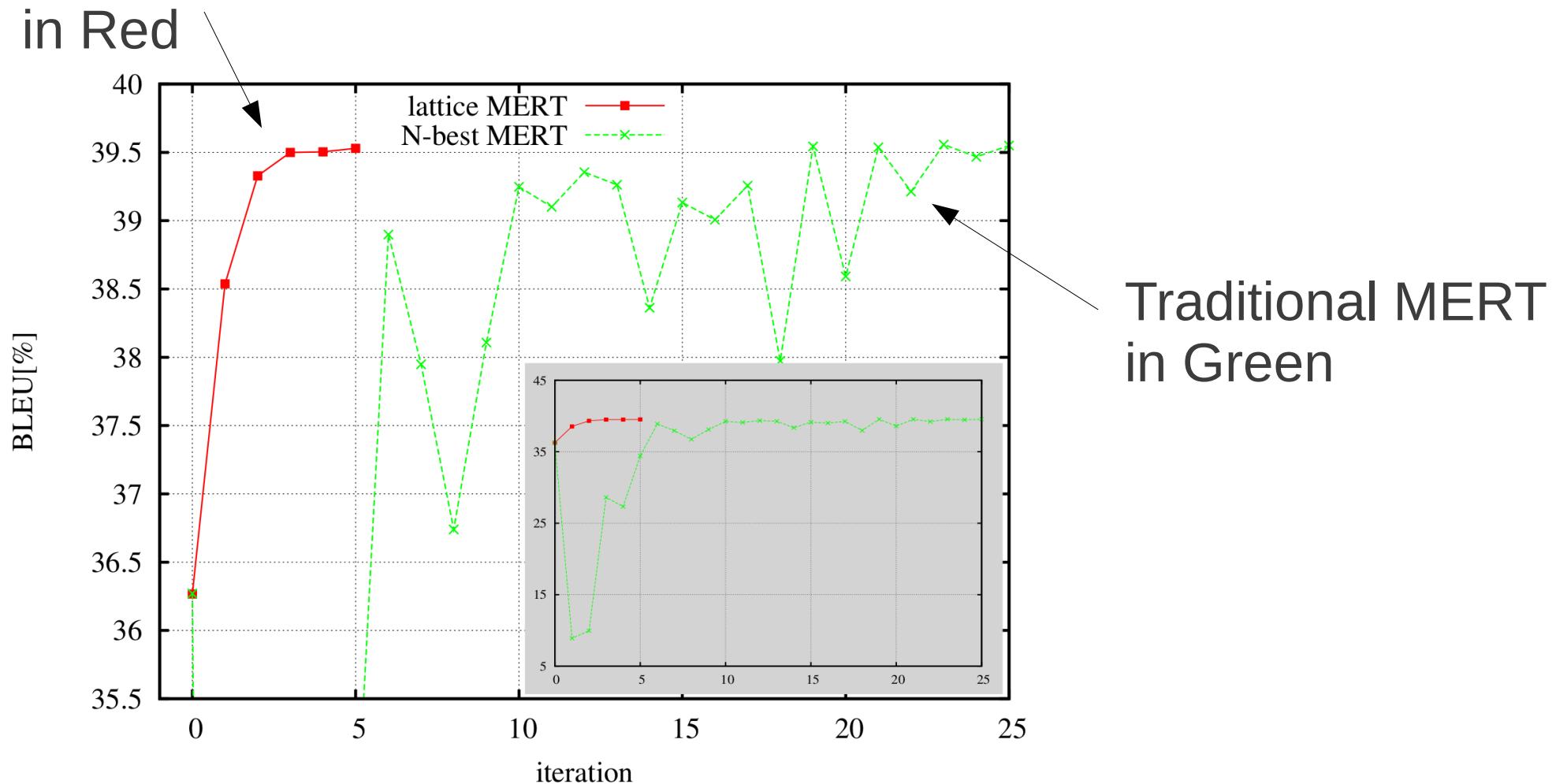
$a=1 \ b=-1$  "Taro visited the Hanako"

$a=0 \ b=1$  "Taro visited Hanako"

$a=-1 \ b=-1$  "the Taro visited Hanako"

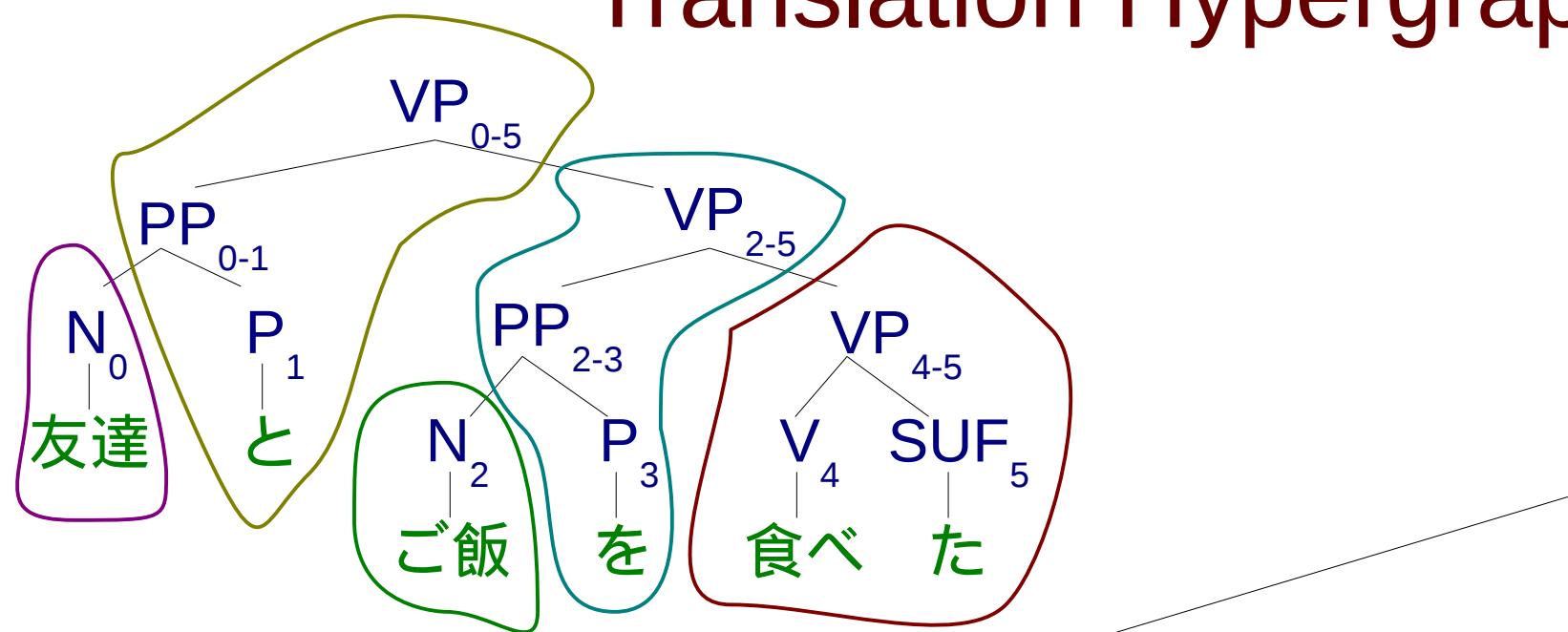
# Improved Stability

Lattice MERT  
in Red



# Hypergraph MERT

# Translation Hypergraph



$x_1$  with  $x_0: 0.56$

$N_0$   
friend: 0.12

my friend: 0.3

$VP_{0-5}$

$x_1 x_0: 0.6$

$N_2$   
a meal: 0.5

$VP_{2-5}$

rice: 0.3

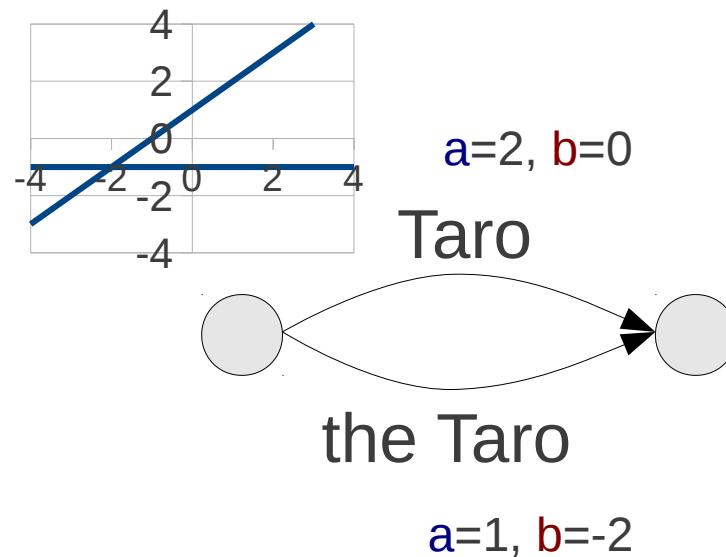
$VP_{4-5}$

ate: 0.5

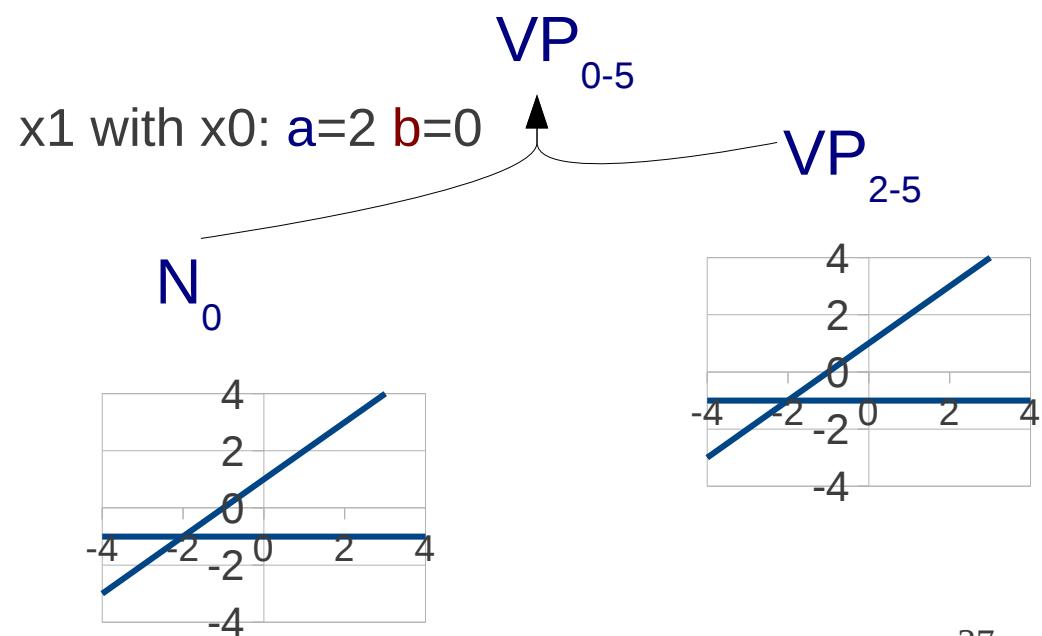
# Hypergraph MERT

- Almost exactly the same as lattice MERT

Lattice MERT



Hypergraph MERT



# Summary

# Summary

- n-best MERT is unstable because of lack of diversity in the n-best list
- This problem can be solved by lattice or hypergraph MERT
- Algorithm finds the upper envelope for each sentence efficiently using dynamic programming