

# Breaking down the Language Barrier with Statistical Machine Translation: 3) Phrase-based MT

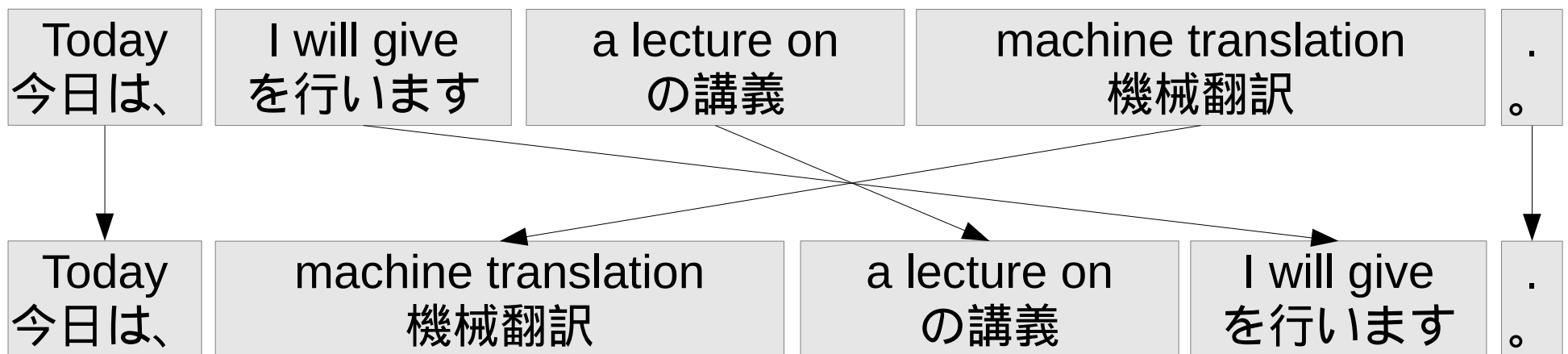
<http://www.phontron.com/class/sentan2014>

Advanced Research Seminar I/III  
Graham Neubig  
2014-2-04

# How does machine translation work?

- Divide sentence into translatable patterns, reorder, combine

Today I will give a lecture on machine translation .



今日は、機械翻訳の講義を行います。

# Assignment

- (Only one assignment this week)
- You are given a baseline machine translation system
  - **LM/Alignment:** Baseline from exercises 1, 2
  - **TM:** Phrases of up to length 4
  - **SM:** Uniform distribution
  - **RM:** Distortion penalty
  - **Reordering Limit:** 6
- Try to improve its accuracy by changing one of the features listed above, or anything else

# Probabilistic Model for Translation

# Formal Definition of Translation

- A translation is defined as (in opposite order)
  - Output sentence  $E$
  - Derivation  $D$
  - Input sentence  $F$

 $E =$ 

hello where is the station

 $D =$  $D_{ep} =$ 

hello

where is

the station

 $D_{fp} =$ 

こんにちは

どこですか

駅は

 $D_o =$ 

0

2

1

 $F =$ 

こんにちは 駅 は どこ です か

# Finding the Best Translation

- We define the “best” translation as the one with the highest posterior probability of  $E$  given  $F$

$$\hat{E} = \operatorname{argmax}_E P(E|F)$$

- We can calculate this by summing over  $D$

$$\hat{E} = \operatorname{argmax}_E \sum_D P(D, E|F)$$

- But this is inefficient, so approximate using the max

$$\hat{E} \approx \operatorname{argmax}_E P(D, E|F)$$

# Probabilistic Modeling of Translation

- We want a probability of **D** and **E** given **F**:  $P(D, E|F)$
- Use Bayes's law and note that  $P(F)$  doesn't affect results

$$P(D, E|F) = P(D, E, F) / P(F) \\ \propto P(D, E, F)$$

- And split the probabilities further

$P(D, E, F) \propto P(E) *$	Language Model
$P(D_{ep} E) *$	Segmentation Model
$P(D_{fp} D_{ep}, E) *$	Translation Model
$P(D_{order} D_{fp}, D_{ep}, E) *$	Reordering Model
$P(F D_{order}, D_{fp}, D_{ep}, E)$	Always $P=1$ ( <b>F</b> is decided by <b>D</b> )

# Language Model

- Calculate the probability of the output words using  $n$ -gram

$$E = \{e_1, \dots, e_I\}$$

$$P(E) = \prod_{i=1}^{I+1} P(e_i | e_{i-N+1}, \dots, e_{i-1})$$

e.g. bigram

$E$  = hello where is the station

$$P(E) = P(\text{hello} | \langle s \rangle) * P(\text{where} | \text{hello}) * P(\text{is} | \text{where}) \\ * P(\text{the} | \text{is}) * P(\text{station} | \text{the}) * P(\langle /s \rangle | \text{station})$$



# Segmentation Model

- Measures the probability of dividing  $E$  into segments

$$D_{ep} = \{ep_1, \dots, ep_K\}$$

$$P(D_{ep} | E)$$

$E =$  hello where is the station  
 $D_{ep} =$ 
hello
where is
the station

- This is less important than other models
- Often just use uniform probability

$$P(D_{ep} | E) = 1 / Z_{ep}$$

- Sometimes use proportional to number of phrases

$$P(D_{ep} | E) = e^{-\alpha_{ep} K} / Z_{ep}$$

(fewer phrases  $\rightarrow$  longer, more reliable phrases)

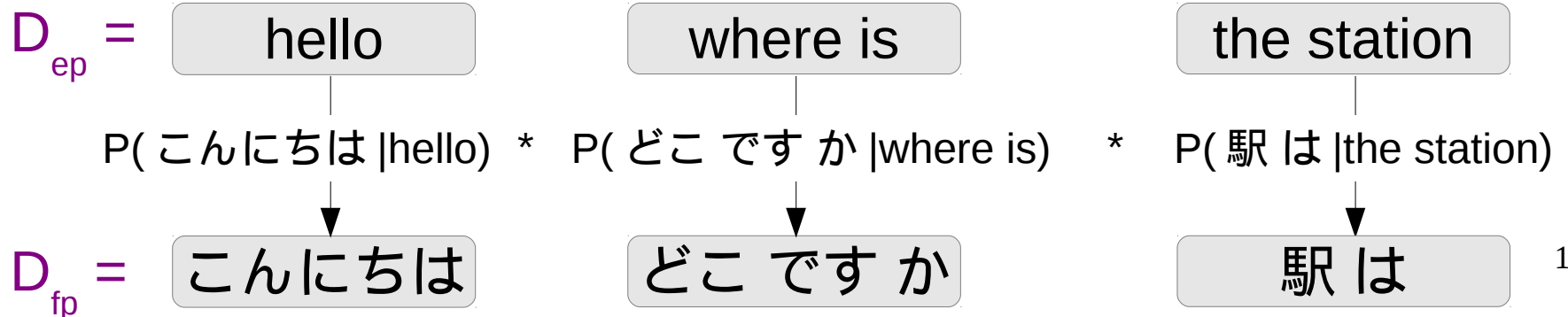
# Translation Model

- Probability of translating phrases  $D_{ep} \rightarrow D_{fp}$ 
  - Because  $P(E|D_{ep}) = 1$ , we can remove  $E$

$$P(D_{fp}|D_{ep}, E) = P(D_{fp}|D_{ep})$$

- We often assume that the translation probability of phrases is independent

$$P(D_{fp}|D_{ep}) = \prod_{k=1}^K P(fp_k|ep_k)$$



# Reordering Model

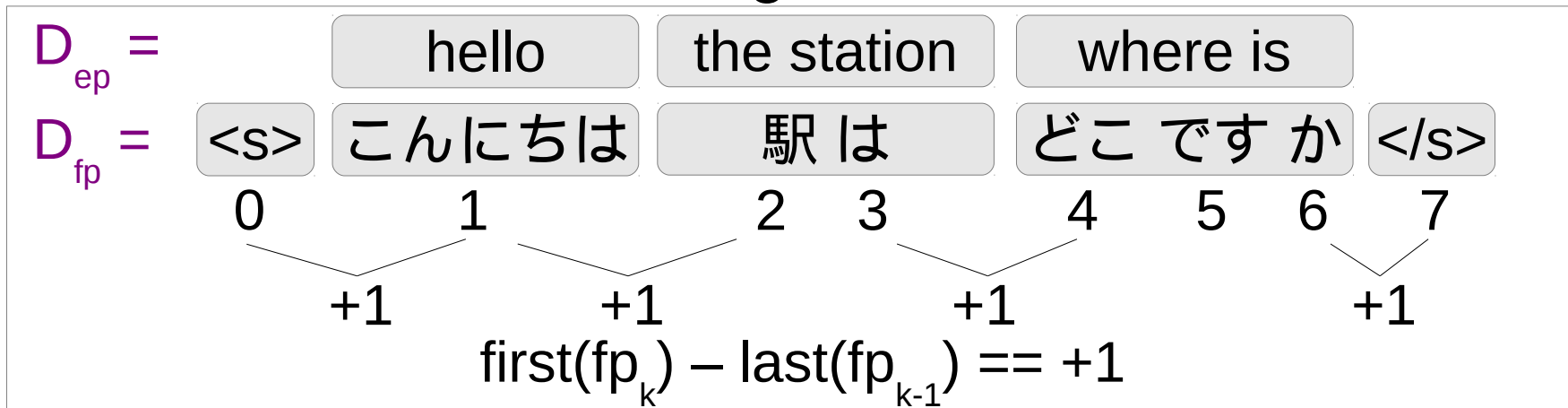
- Probability of choosing a particular ordering

$$P(D_o | D_{fp}, D_{ep}, E) = P(D_o | D_{fp}, D_{ep})$$

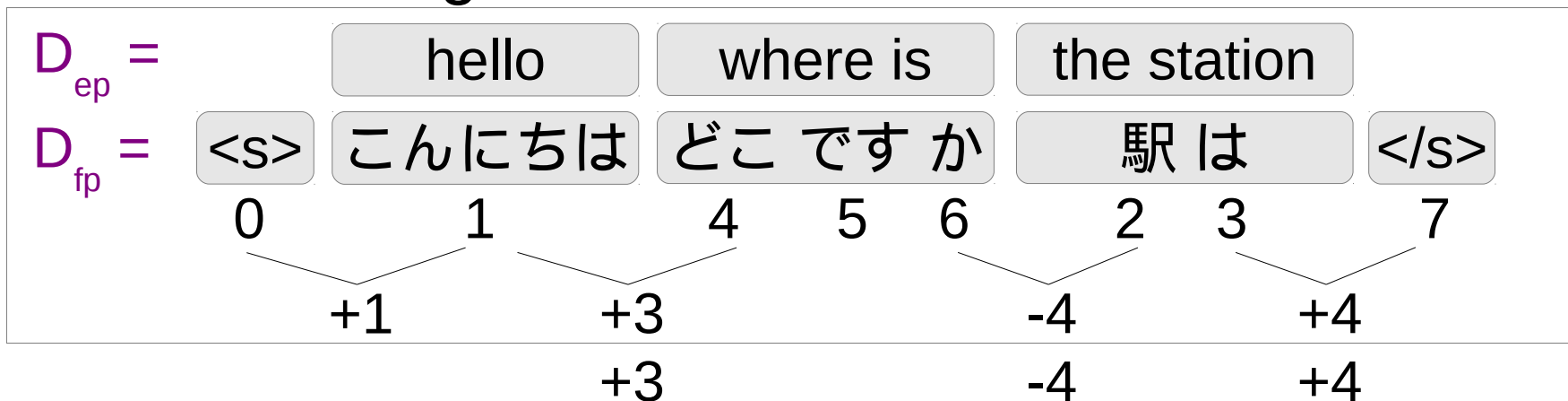
$D_{ep} =$	hello	where is	the station
$D_{fp} =$	こんにちは	どこですか	駅は
$D_o =$	0	2	1

# Reordering Model: Distortion Penalty (1)

- Think about no reordering:



- With reordering:



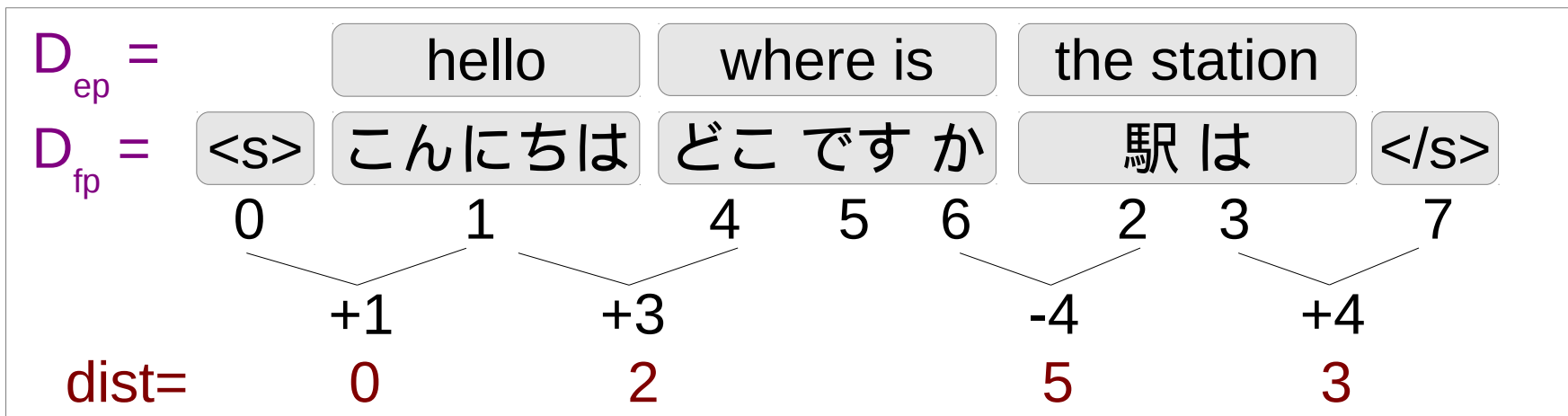
$$dist(fp_{k-1}, fp_k) = |first(fp_k) - last(fp_{k-1}) - 1|$$

- Distortion is distance from +1: 

# Reordering Model: Distortion Penalty (2)

- Distortion is the distance from +1:

$$\text{dist}(fp_{k-1}, fp_k) = |\text{first}(fp_k) - \text{last}(fp_{k-1}) - 1|$$

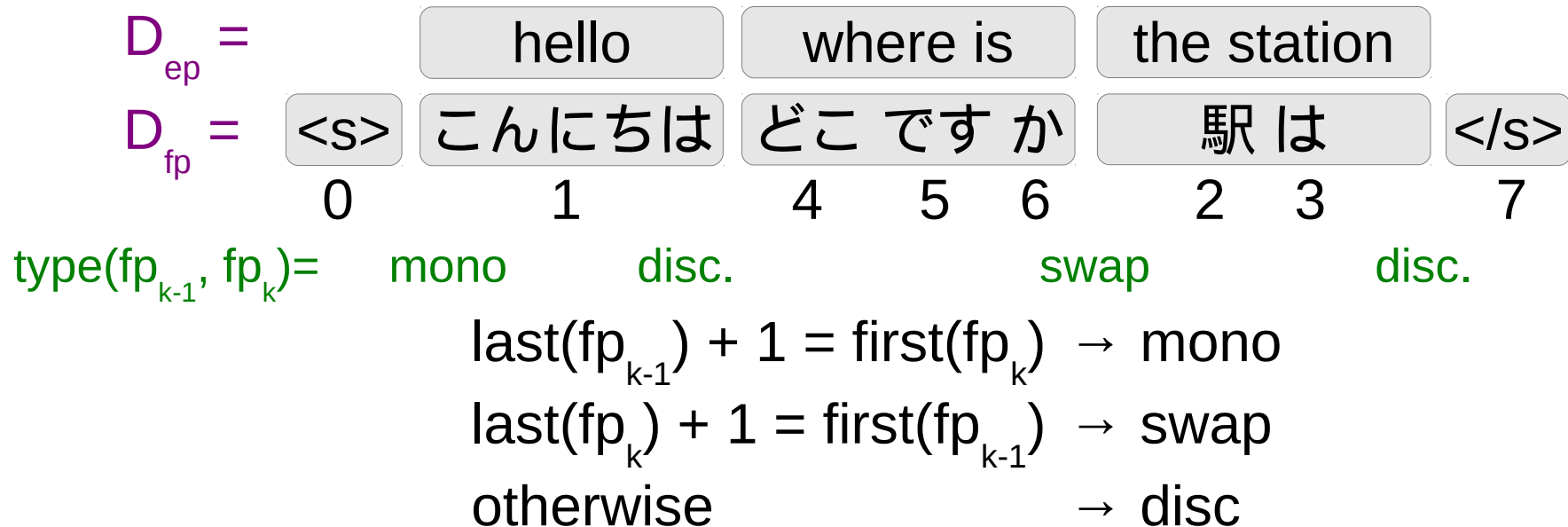


- We put an exponential penalty on distortion:

$$P(D_o | D_{fp}, D_{ep}) = \frac{\prod_{k=1}^{K+1} e^{-\alpha_o \text{dist}(fp_{k-1}, fp_k)}}{Z_o}$$

# Reordering Model: Lexicalized Reordering Probability

- Each phrase has a reordering type



- Calculate probability from training data and multiply

$$P(D_o | D_{fp}, D_{ep}) = \frac{\prod_{k=1}^{K+1} P(\text{type}(fp_{k-1}, fp_k) | fp_{k-1}, ep_{k-1})}{Z_o}$$

# Putting Everything Together

$$P(D, E, F) \propto P(E) *$$

Language Model

$$P(D_{ep} | E) *$$

Segmentation Model

$$P(D_{fp} | D_{ep}, E) *$$

Translation Model

$$P(D_{order} | D_{fp}, D_{ep}, E)$$

Reordering Model

$D_{ep} =$	hello	where is	the station
$D_{fp} =$	こんにちは	どこですか	駅は
$D_o =$	0	2	1

LM (bigram) =  $P(\text{hello} | \langle s \rangle) * P(\text{where} | \text{hello}) * P(\text{is} | \text{where}) * P(\text{the} | \text{is}) * P(\text{station} | \text{the}) * P(\langle /s \rangle | \text{station})$

SM (expon) =  $e^{-\alpha_{ep}} * e^{-\alpha_{ep}} * e^{-\alpha_{ep}}$

TM =  $P(\text{こんにちは} | \text{hello}) * P(\text{どこですか} | \text{where is}) * P(\text{駅は} | \text{the station})$

RM (distort) =  $e^{-\alpha_o * 0} * e^{-\alpha_o * 2} * e^{-\alpha_o * 5} * e^{-\alpha_o * 3}$

# Log Probabilities

$\log P(D, E, F) \propto \log P(E) +$	Language Model
$\log P(D_{ep}   E) +$	Segmentation Model
$\log P(D_{fp}   D_{ep}, E) +$	Translation Model
$\log P(D_{order}   D_{fp}, D_{ep}, E)$	Reordering Model

$D_{ep} =$	hello	where is	the station
$D_{fp} =$	こんにちは	どこですか	駅は
$D_o =$	0	2	1

LM (bigram) =  $\log P(\text{hello} | \langle s \rangle) + \log P(\text{where} | \text{hello}) + \log P(\text{is} | \text{where}) + \log P(\text{the} | \text{is}) + \log P(\text{station} | \text{the}) + \log P(\langle /s \rangle | \text{station})$

SM (expon) =  $-\alpha_{ep} + -\alpha_{ep} + -\alpha_{ep}$

TM =  $\log P(\text{こんにちは} | \text{hello}) + \log P(\text{どこですか} | \text{where is}) + \log P(\text{駅は} | \text{the station})$

RM (distort) =  $-\alpha_o * 0 + -\alpha_o * 2 + -\alpha_o * 5 + -\alpha_o * 3$



# Search for Machine Translation

# Search for Machine Translation

- We want to find the best scoring hypothesis

$$\hat{E} = \operatorname{argmax}_E P(D, E | F)$$

- **Problem:** Millions of possible hypotheses for one sentence!
- **Solution:** Efficient dynamic programming and approximate search algorithms.

# Starting Simple

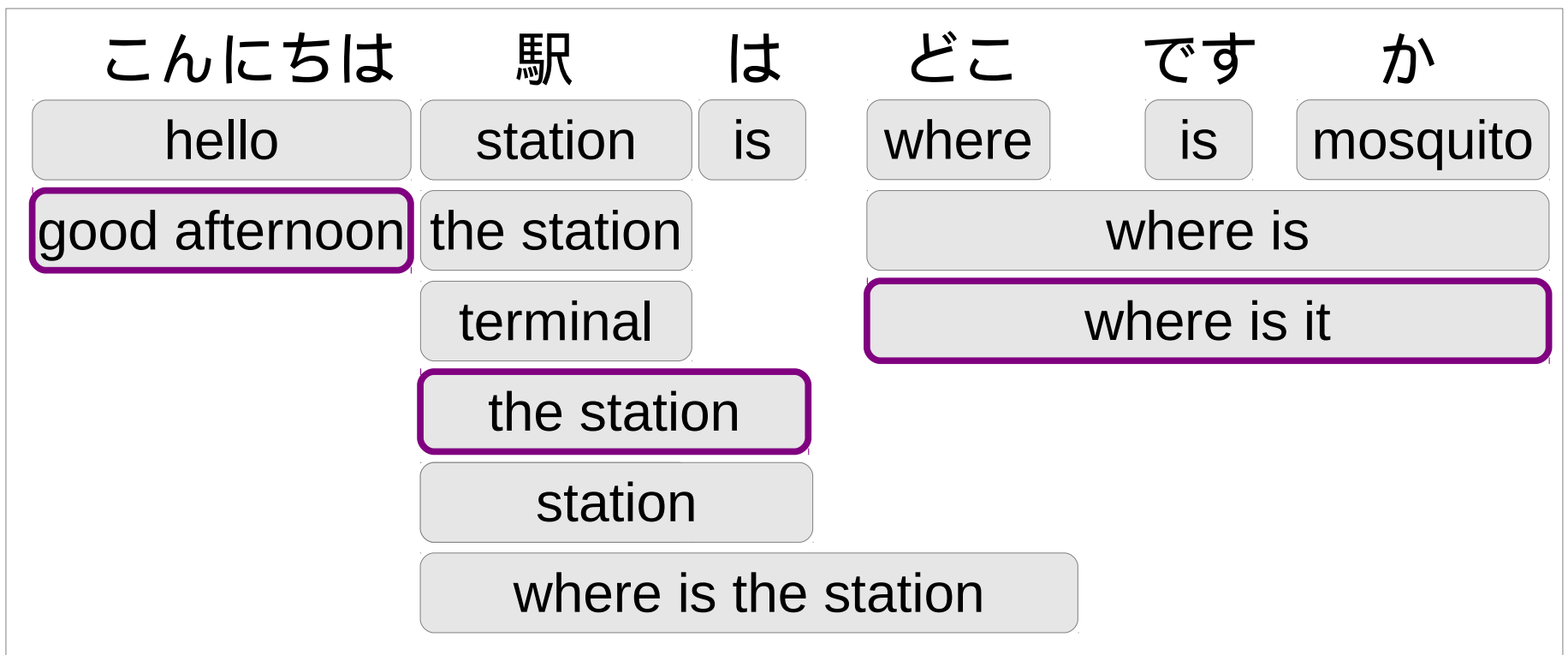
- What do we do when we only have the translation model probability?

$$P(D, E, F) \approx P(D_{fp} | D_{ep})$$

(No reordering for now)

# Simple Search

- Given an input
- Expand all of the possible translations



- Find the set of translations maximizing

$$P(D_{fp} | D_{ep}) = \prod_{k=1}^K P(fp_k | ep_k)$$

but how?

# This Man Has an Answer!

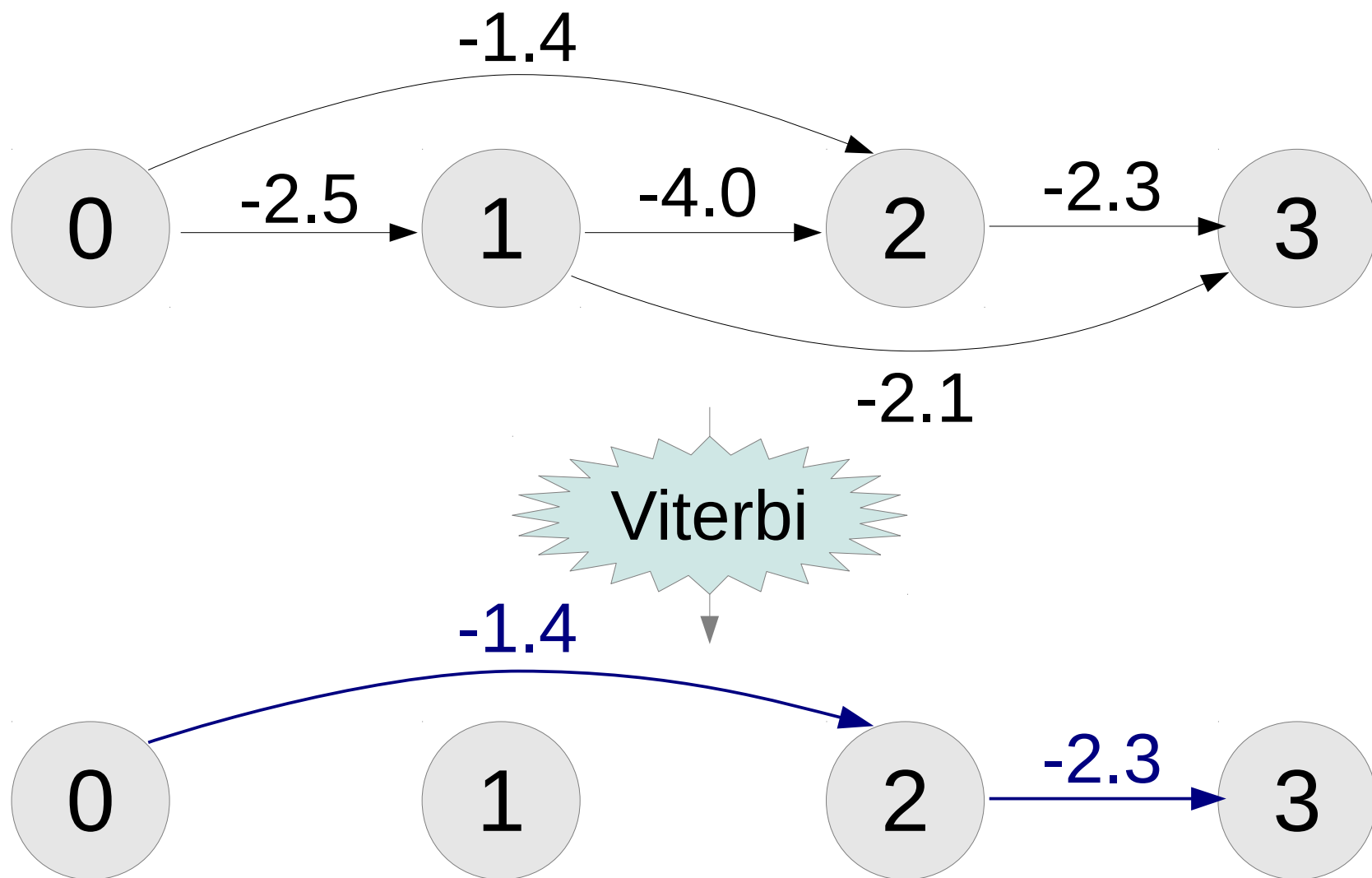


**Andrew Viterbi**  
(Professor UCLA → Founder of Qualcomm)

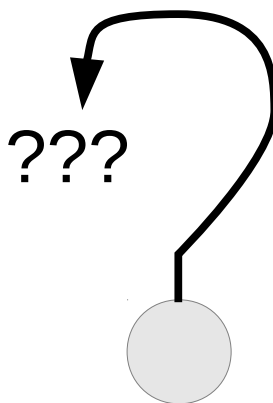
# Viterbi Algorithm

# The Viterbi Algorithm

- Efficient way to find the **highest scoring path** in a graph



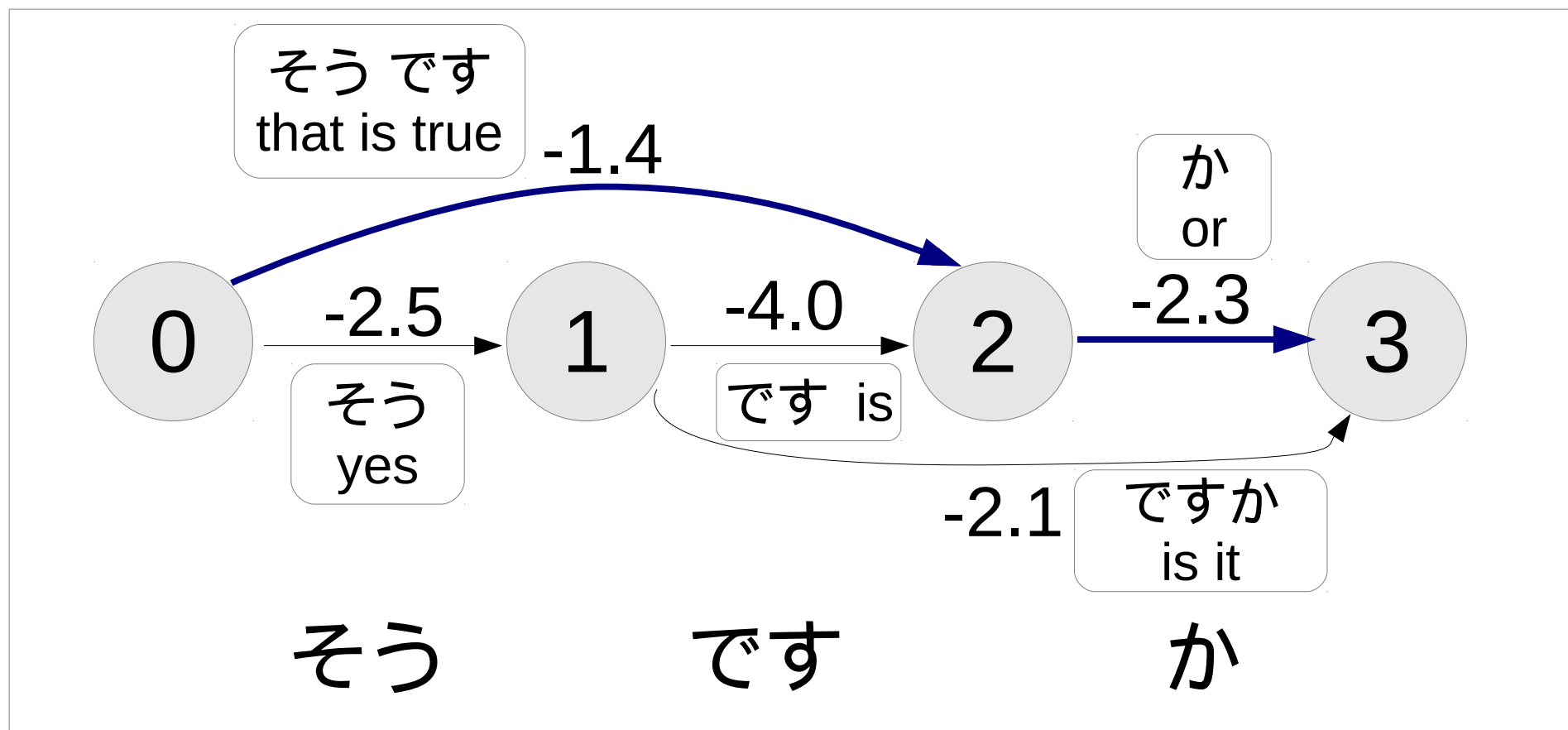
# Graph?! What?!



(Let Me Explain!)

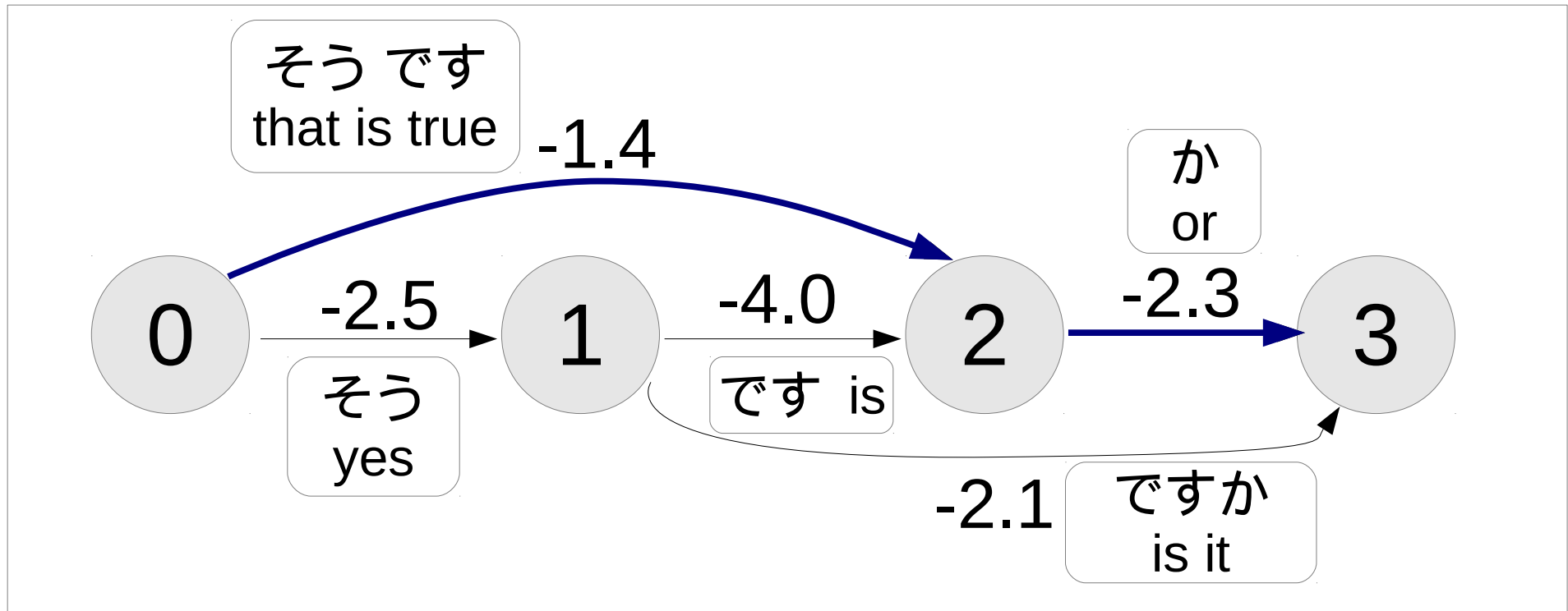


# Translations as Graphs



- Each node is a position in the sentence
- Each edge is a phrase
- Each path is a full translation

# Graph Weights



- Each edge has a weight equal to  $\log P(fp_k | ep_k)$
- Each path has a weight equal to sum of edges

$$\log P(D_{fp} | D_{ep}) = \sum_{k=1}^K \log P(fp_k | ep_k)$$

- Highest scoring path is best translation!

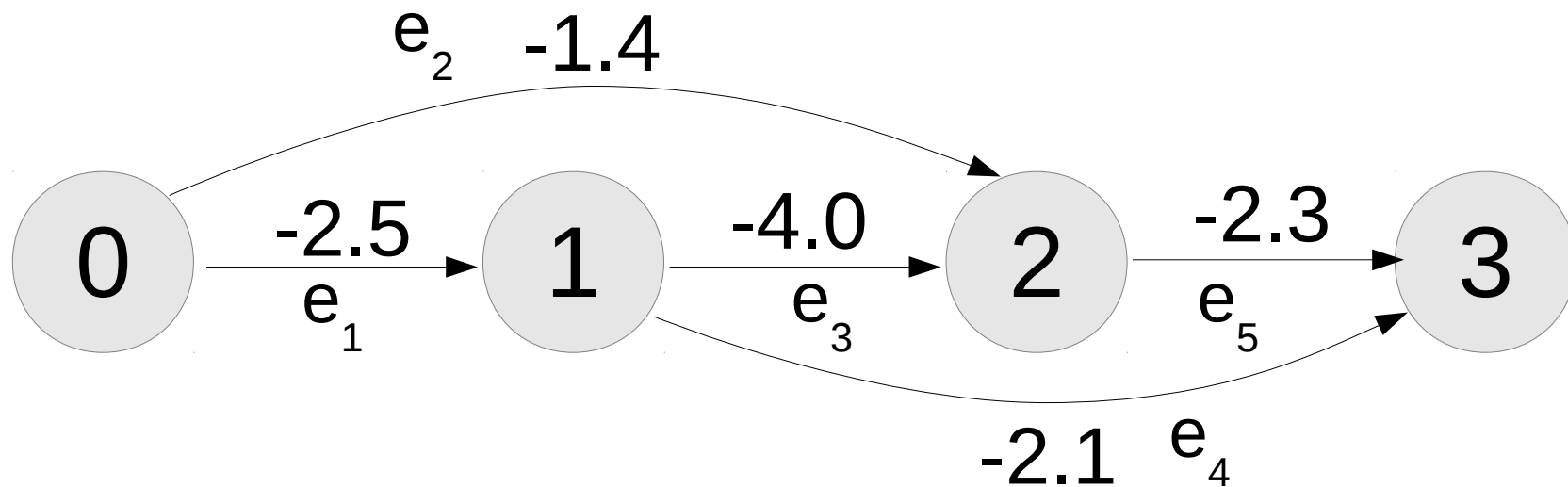
# Ok Viterbi, Tell Me More!

- The Viterbi Algorithm has two steps
  - In **forward** order, find the score of the best path to each node
  - In **backward** order, create the best path



# Forward Step

## Forward Step



$best\_score[0] = 0$

**for each** *node* in the *graph* (ascending order)

$best\_score[node] = -\infty$

**for each** incoming *edge* of *node*

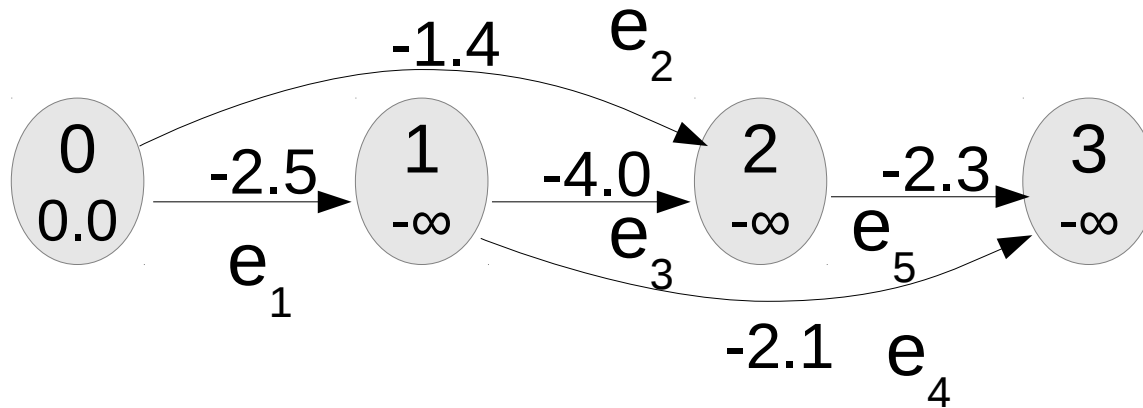
$score = best\_score[edge.prev\_node] + edge.score$

**if**  $score > best\_score[node]$

$best\_score[node] = score$

$best\_edge[node] = edge$

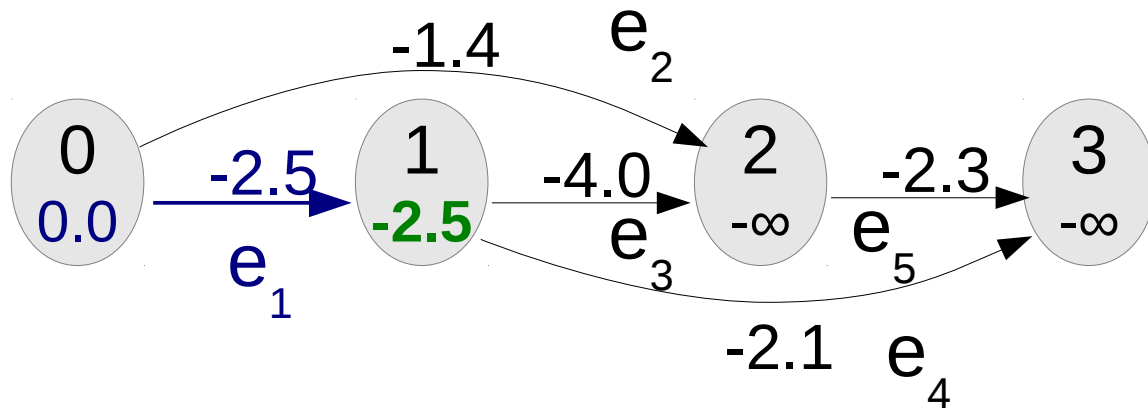
# Example:



Initialize:

$\text{best\_score}[0] = 0$

# Example:



## Initialize:

$$\text{best\_score}[0] = 0$$

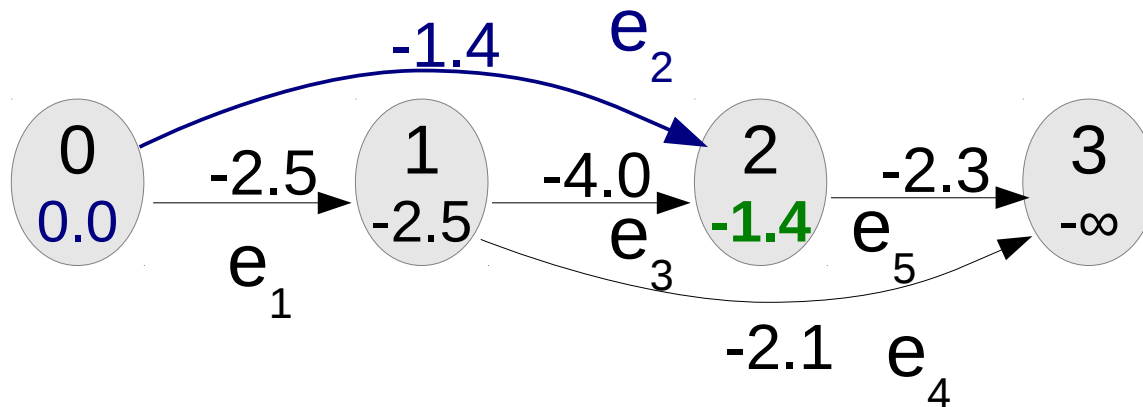
## Check $e_1$ :

$$\text{score} = 0 + -2.5 = -2.5 (> -\infty)$$

$$\text{best\_score}[1] = -2.5$$

$$\text{best\_edge}[1] = e_1$$

# Example:



## Initialize:

$$\text{best\_score}[0] = 0$$

## Check $e_1$ :

$$\text{score} = 0 + -2.5 = -2.5 (> -\infty)$$

$$\text{best\_score}[1] = -2.5$$

$$\text{best\_edge}[1] = e_1$$

## Check $e_2$ :

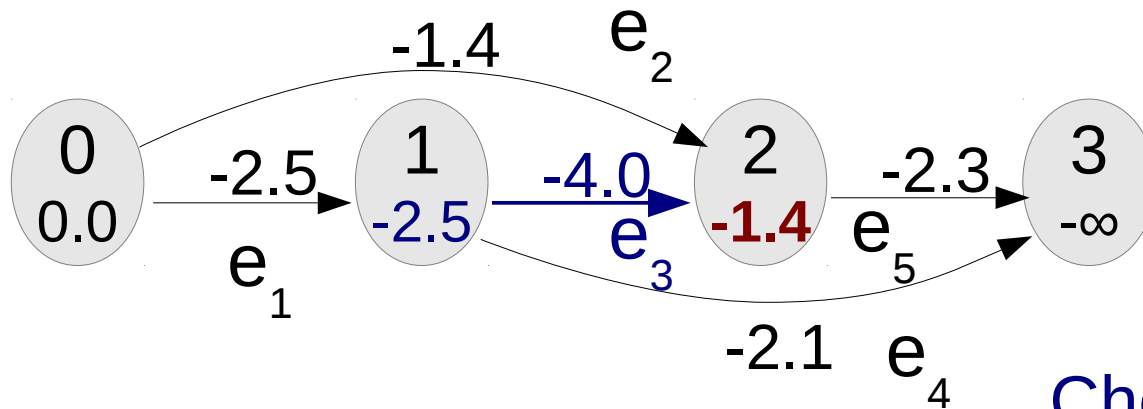
$$\text{score} = 0 + -1.4 = -1.4 (> -\infty)$$

$$\text{best\_score}[2] = -1.4$$

$$\text{best\_edge}[2] = e_2$$



# Example:



## Initialize:

$\text{best\_score}[0] = 0$

## Check $e_1$ :

$\text{score} = 0 + -2.5 = -2.5 (> -\infty)$

$\text{best\_score}[1] = -2.5$

$\text{best\_edge}[1] = e_1$

## Check $e_2$ :

$\text{score} = 0 + -1.4 = -1.4 (> -\infty)$

$\text{best\_score}[2] = -1.4$

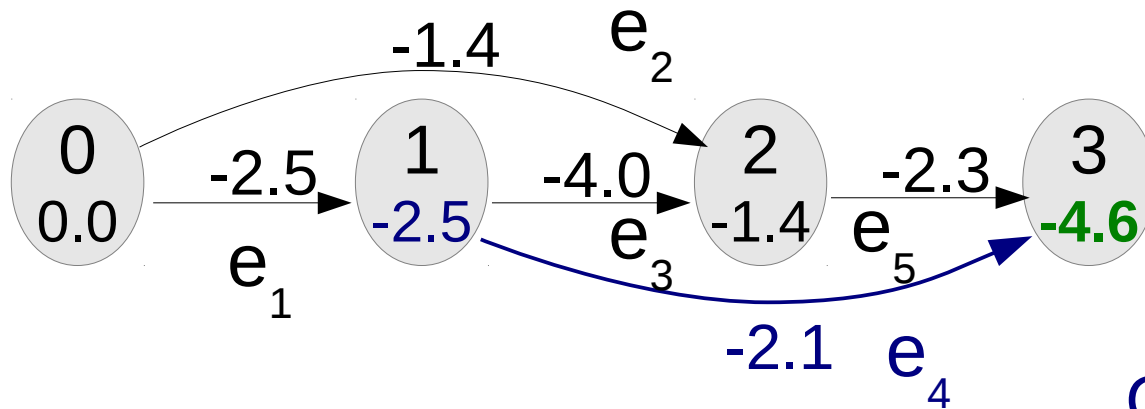
$\text{best\_edge}[2] = e_2$

## Check $e_3$ :

$\text{score} = -2.5 + -4.0 = -6.5 (< -1.4)$

**No change!**

# Example:



## Initialize:

$$\text{best\_score}[0] = 0$$

## Check $e_1$ :

$$\text{score} = 0 + -2.5 = -2.5 (> -\infty)$$

$$\text{best\_score}[1] = -2.5$$

$$\text{best\_edge}[1] = e_1$$

## Check $e_2$ :

$$\text{score} = 0 + -1.4 = -1.4 (> -\infty)$$

$$\text{best\_score}[2] = -1.4$$

$$\text{best\_edge}[2] = e_2$$

## Check $e_3$ :

$$\text{score} = -2.5 + -4.0 = -6.5 (< -1.4)$$

No change!

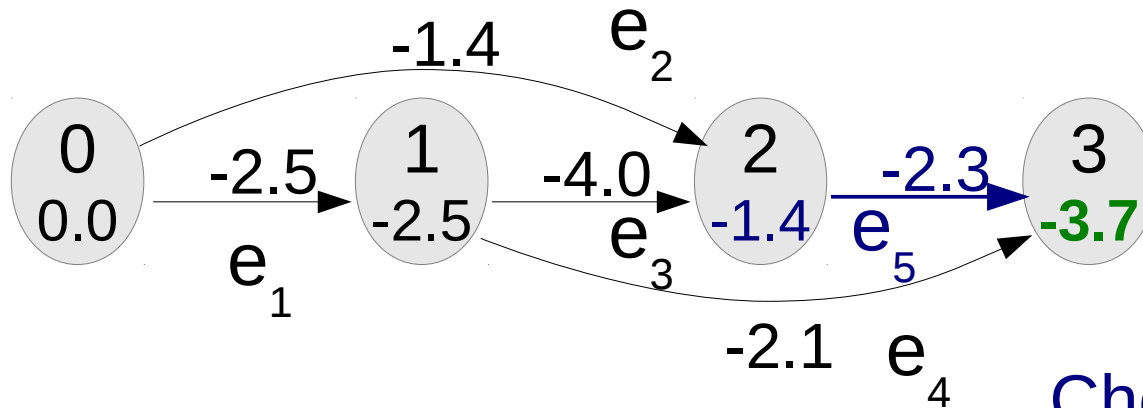
## Check $e_4$ :

$$\text{score} = -2.5 + -2.1 = -4.6 (> -\infty)$$

$$\text{best\_score}[3] = -4.6$$

$$\text{best\_edge}[3] = e_4$$

# Example:



## Initialize:

$\text{best\_score}[0] = 0$

## Check $e_1$ :

$\text{score} = 0 + -2.5 = -2.5 (> -\infty)$

$\text{best\_score}[1] = -2.5$

$\text{best\_edge}[1] = e_1$

## Check $e_2$ :

$\text{score} = 0 + -1.4 = -1.4 (> -\infty)$

$\text{best\_score}[2] = -1.4$

$\text{best\_edge}[2] = e_2$

## Check $e_3$ :

$\text{score} = -2.5 + -4.0 = -6.5 (< -1.4)$

**No change!**

## Check $e_4$ :

$\text{score} = -2.5 + -2.1 = -4.6 (> -\infty)$

~~$\text{best\_score}[3] = -4.6$~~

~~$\text{best\_edge}[3] = e_4$~~

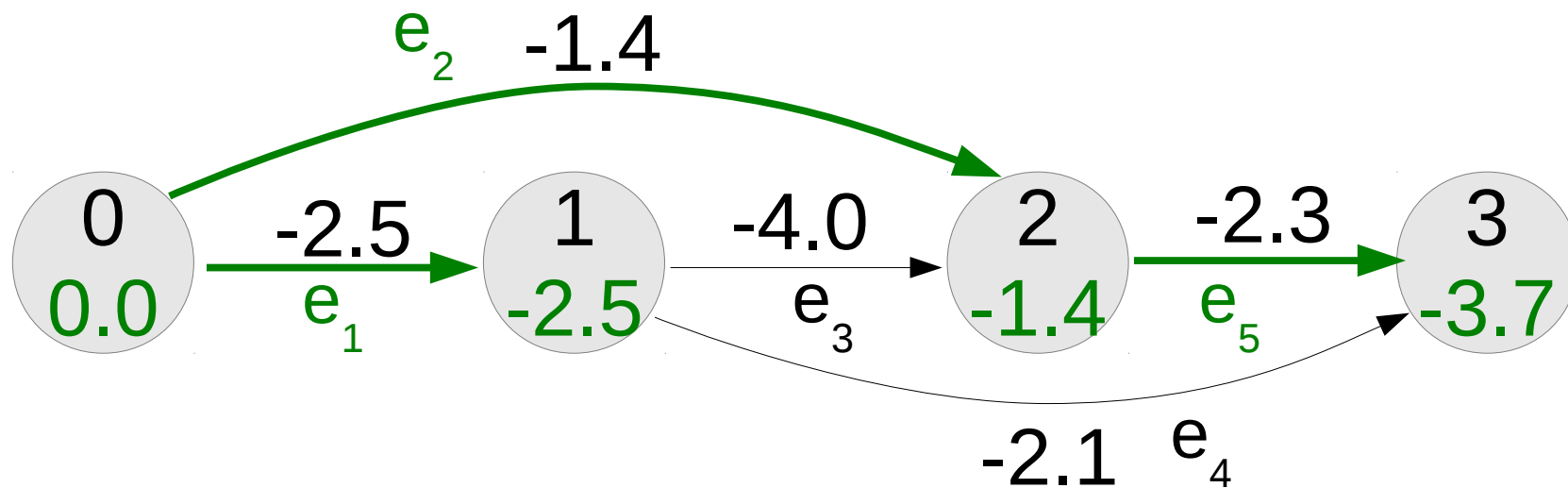
## Check $e_5$ :

$\text{score} = -1.4 + -2.3 = -3.7 (> -4.6)$

$\text{best\_score}[3] = -3.7$

$\text{best\_edge}[3] = e_5$

## Result of Forward Step

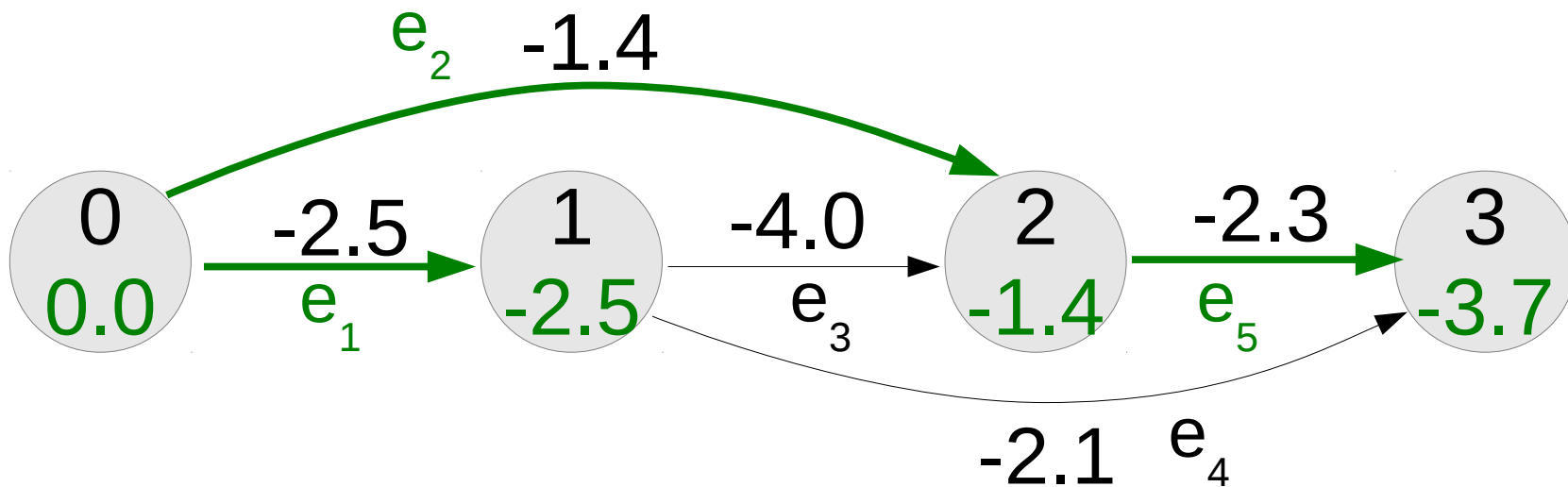


$best\_score = ( 0.0, -2.5, -1.4, -3.7 )$

$best\_edge = ( NULL, e_1, e_2, e_5 )$

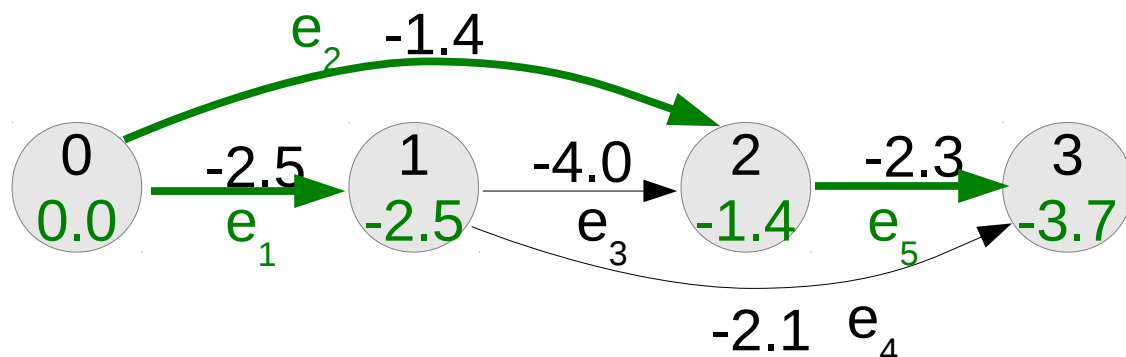
# Backward Step

## Backward Step



```
best_path = []  
next_edge = best_edge[best_edge.length - 1]  
while next_edge != NULL  
    add next_edge to best_path  
    next_edge = best_edge[next_edge.prev_node]  
reverse best_path
```

# Example of Backward Step

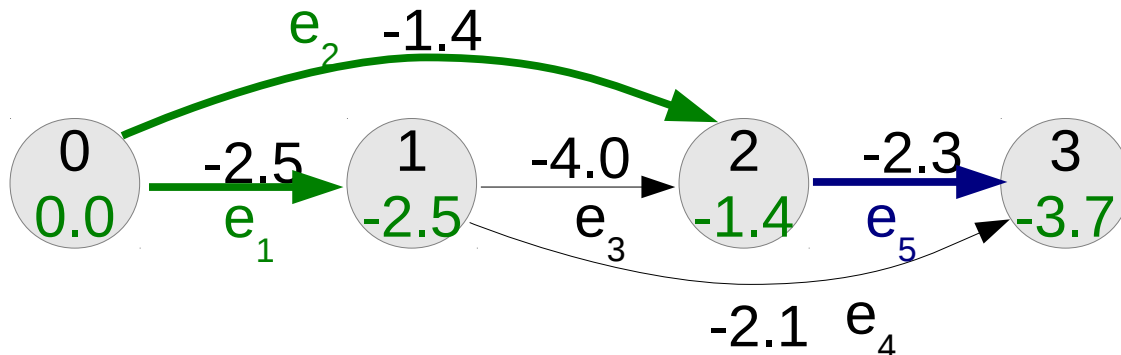


Initialize:

$best\_path = []$

$next\_edge = best\_edge[3] = e_5$

# Example of Backward Step



## Initialize:

$best\_path = []$

$next\_edge = best\_edge[3] = e_5$

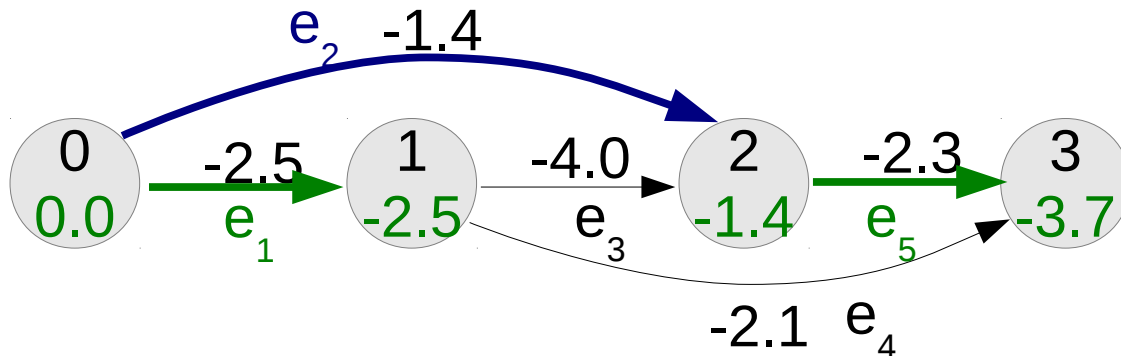
## Process $e_5$ :

$best\_path = [e_5]$

$next\_edge = best\_edge[2] = e_2$



# Example of Backward Step



## Initialize:

$best\_path = []$   
 $next\_edge = best\_edge[3] = e_5$

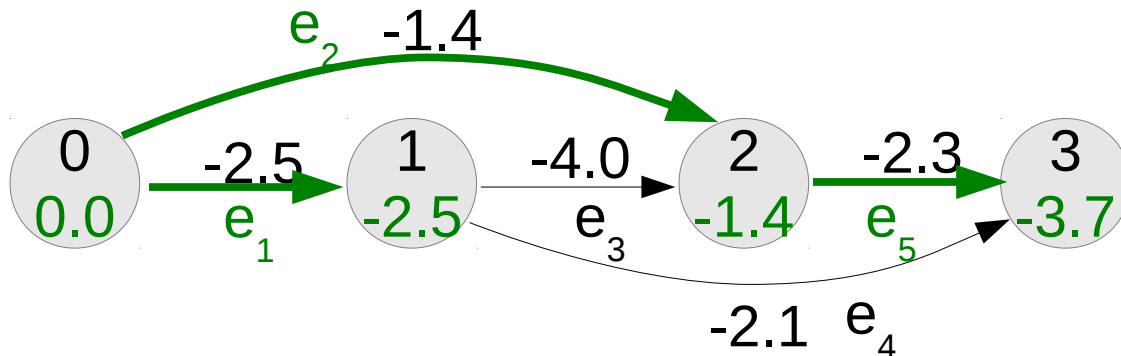
## Process $e_2$ :

$best\_path = [e_5, e_2]$   
 $next\_edge = best\_edge[0] = NULL$

## Process $e_5$ :

$best\_path = [e_5]$   
 $next\_edge = best\_edge[2] = e_2$

# Example of Backward Step



## Initialize:

$best\_path = []$   
 $next\_edge = best\_edge[3] = e_5$

## Process $e_5$ :

$best\_path = [e_5]$   
 $next\_edge = best\_edge[2] = e_2$

## Process $e_2$ :

$best\_path = [e_5, e_2]$   
 $next\_edge = best\_edge[0] = NULL$

## Reverse:

$best\_path = [e_2, e_5]$

# Search with a Language Model

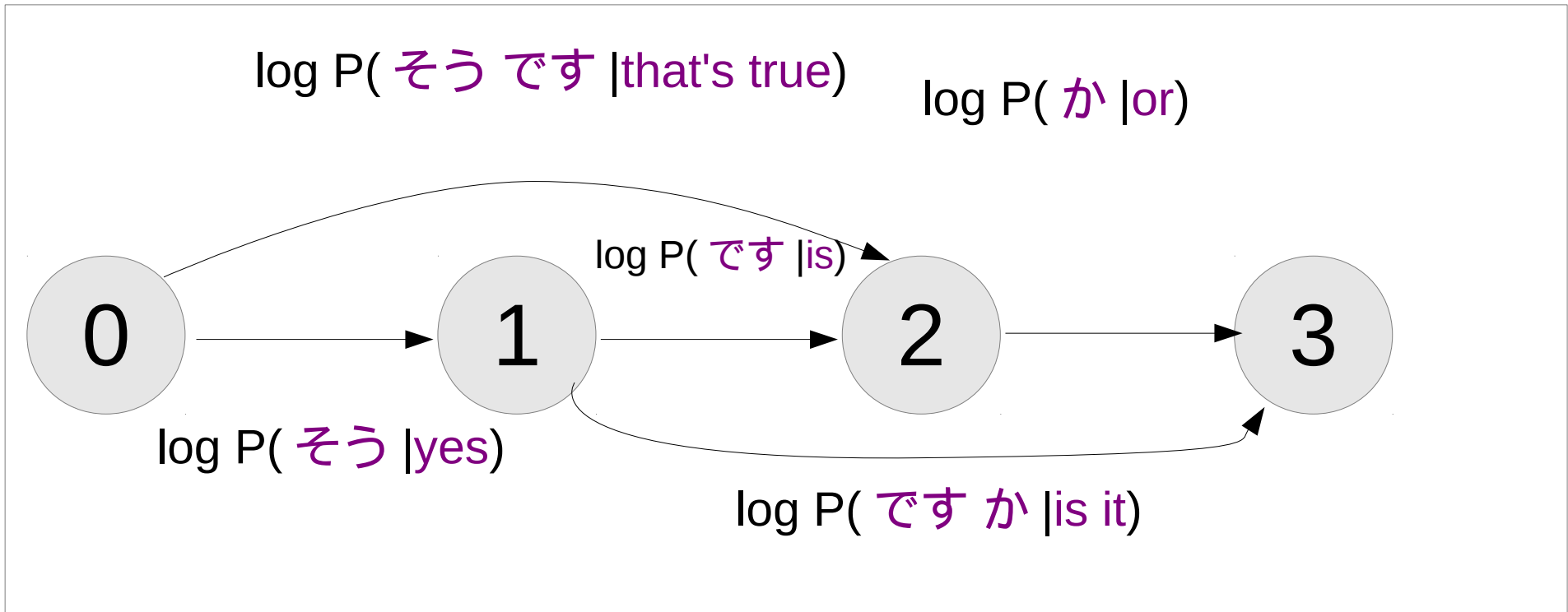
# Language Model Probabilities

- Next let's add language model probabilities

$$P(D, E, F) \approx P(E) P(D_{fp} | D_{ep})$$

(still no reordering)

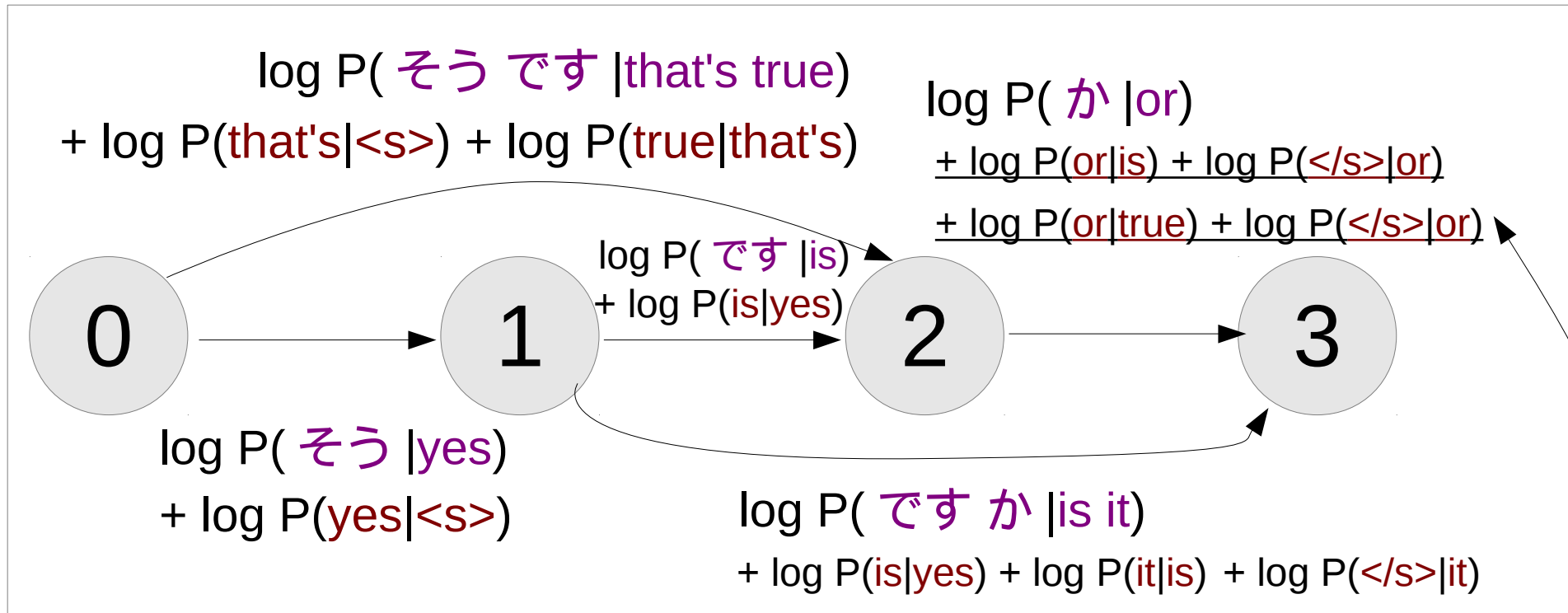
# Graph Weights Review



- Each edge has a weight equal to  $\log P(fp_k | ep_k)$
- Each path has a weight equal to sum of edges

$$\log P(D_{fp} | D_{ep}) = \sum_{k=1}^K \log P(fp_k | ep_k)$$

# Adding Language Model Weights?



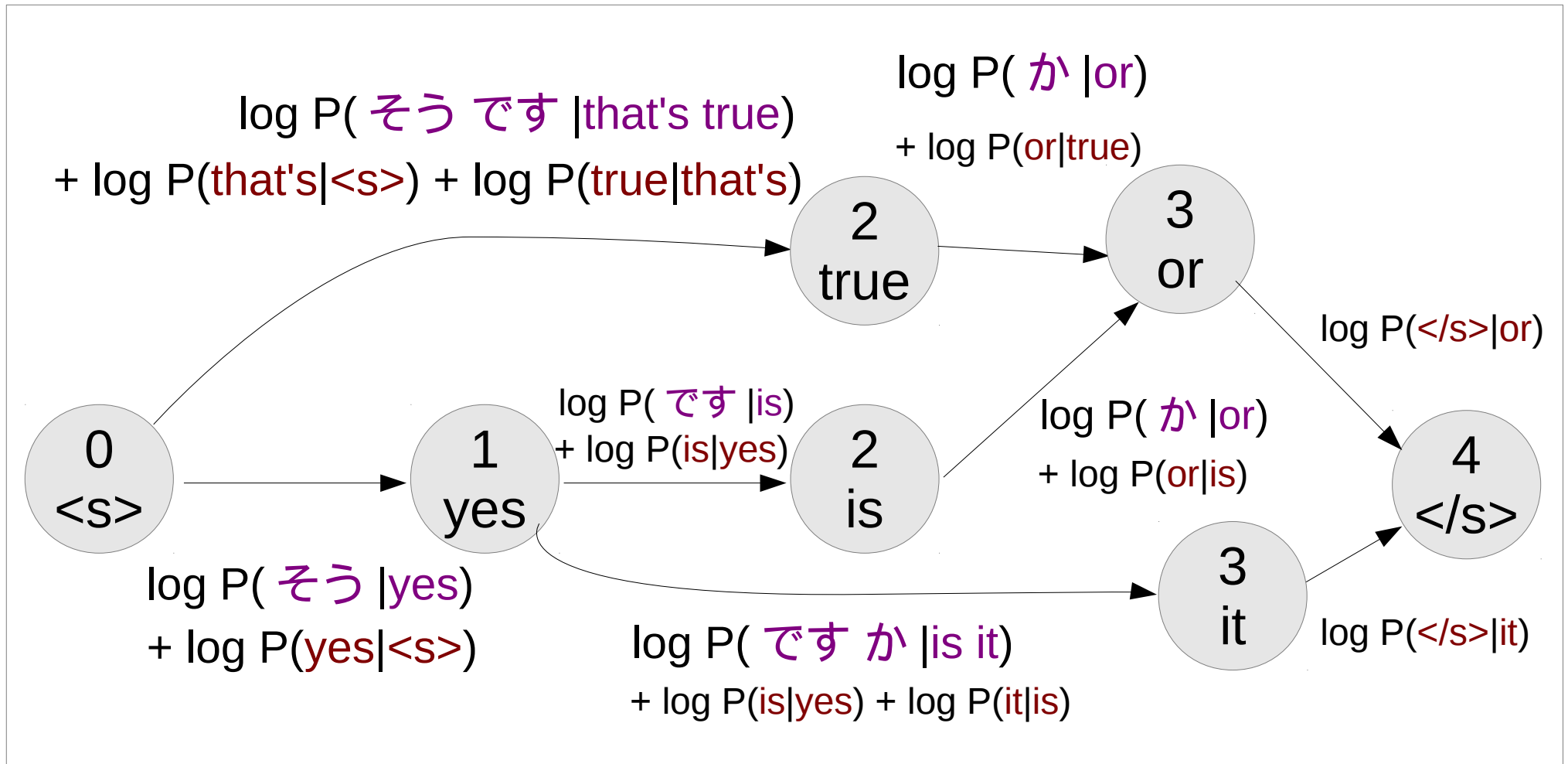
- How do we add **word bigrams**?

PROBLEM

We cannot decide which history to use!

# Augmenting the States

- Remember the last translated word in every state!



- If using longer n-grams, remember n-1 words

# Search with Reordering



# Reordering

- Next let's allow reordering and add probabilities

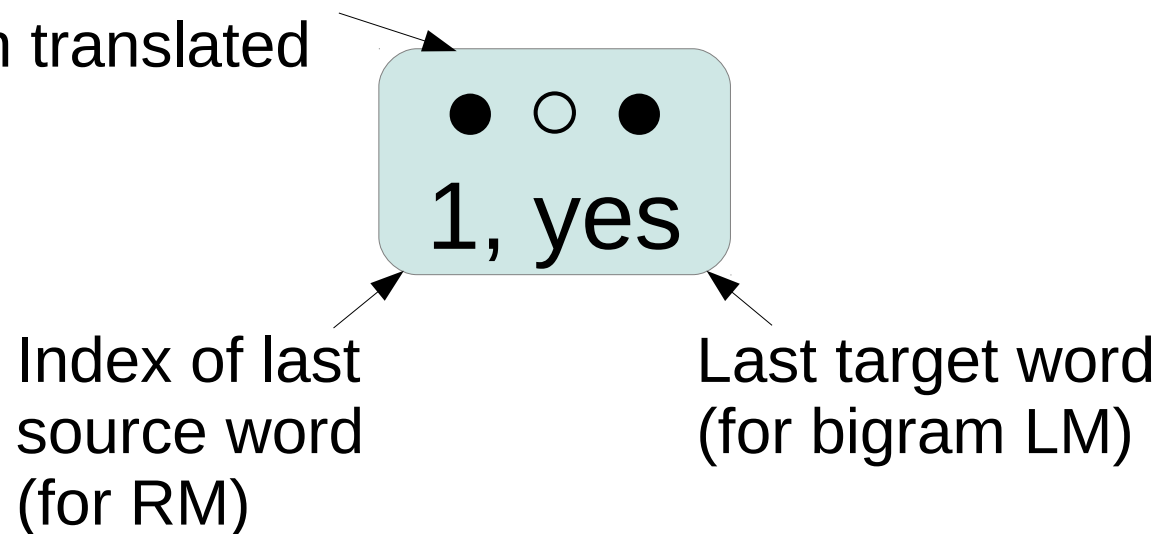
$$P(D, E, F) \approx P(E) P(D_{fp} | D_{ep}) P(D_o | D_{fp}, D_{ep})$$

- What order do we calculate in?
- Basic idea:
  - Generate target sentence from left to right
  - Remember which words have been covered, last word translated

# State Example

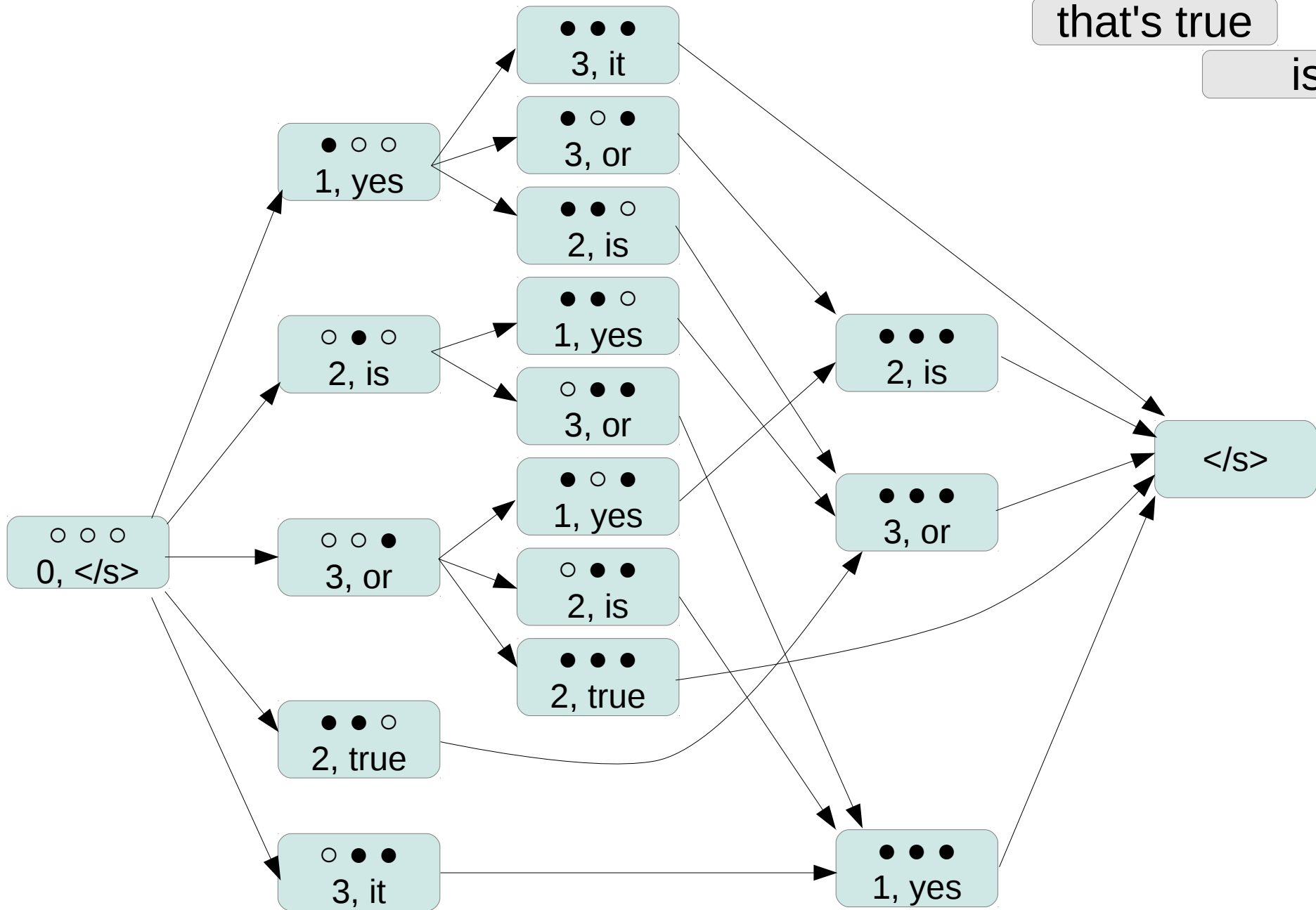
- Each state includes information about

Which words  
have been translated



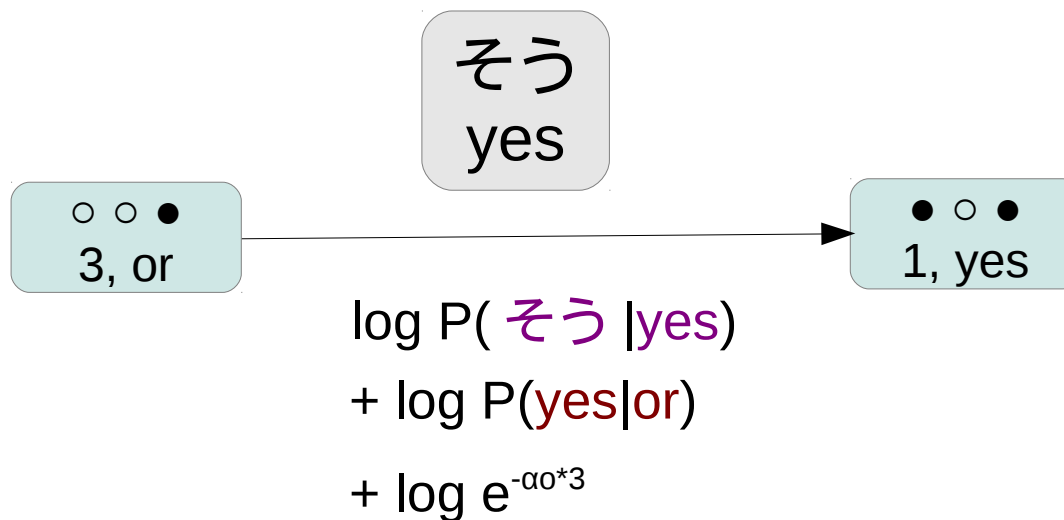
# Search Example

そう	です	か
yes	is	or
that's true		
is it		



# Calculating Edge Probabilities

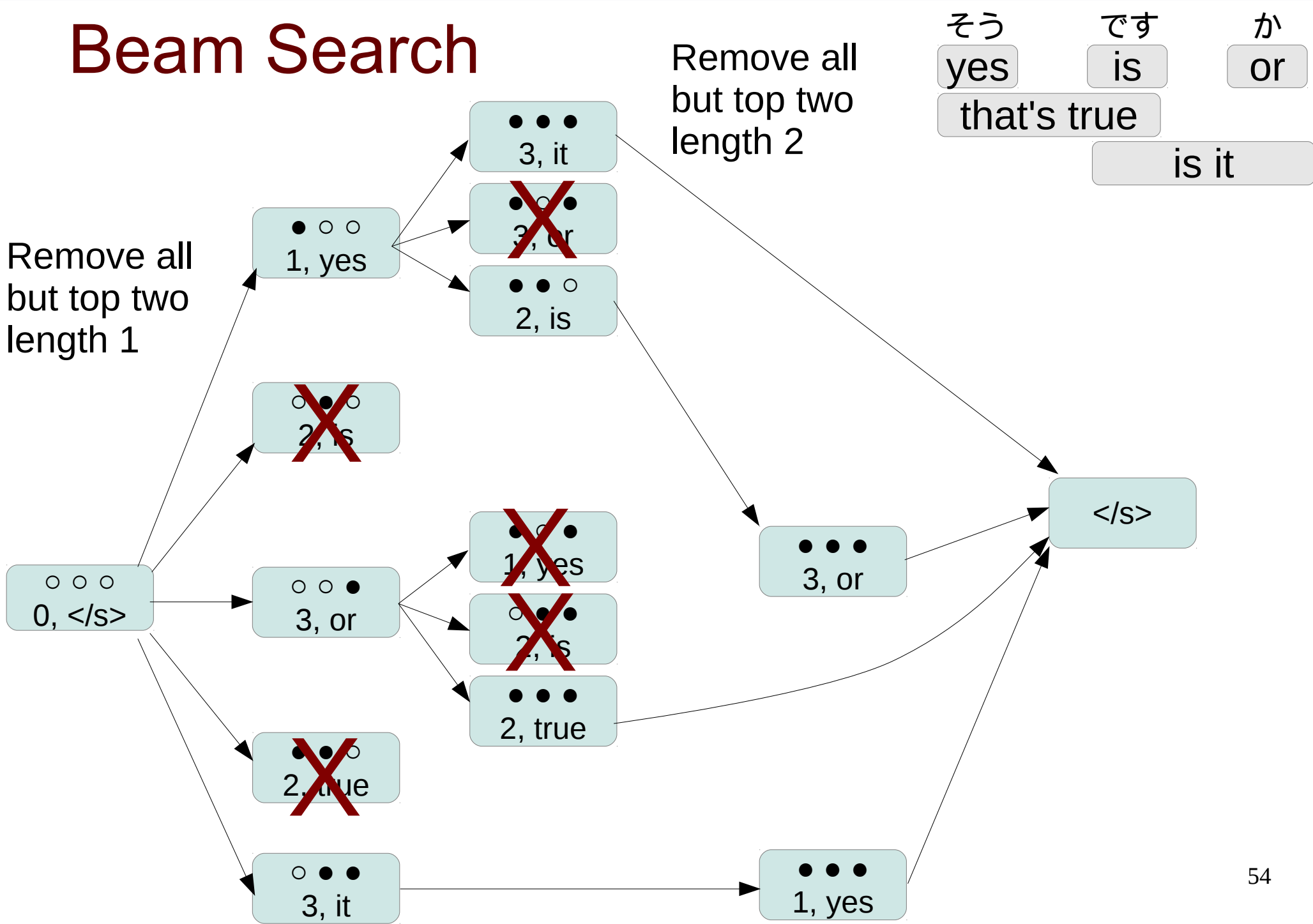
- Can calculate all probabilities based on the nodes/edge



# Problem!

- Exact search for phrase-based MT is NP-hard!
- Make two approximations:
  - Remove low-scoring hypotheses that have the same number of words translated (“Beam Search”)
  - Limit maximum distortion

# Beam Search



# Stack Decoding

- We can also view this as “stacks” based on the number of words

## 0 words

○ ○ ○  
0, </s> ○

## 1 words

● ○ ○ ○  
1, yes ○

○ ○ ● ○  
3, or ○

○ ● ○ ○  
2, is

## 2 words

○ ● ● ○  
3, it ○

● ● ○ ○  
2, is ○

● ● ○ ○  
2, true

● ○ ● ○  
3, or

● ○ ● ○  
1, yes

○ ● ● ○  
2, is

## 3 words

● ● ● ○  
3, it

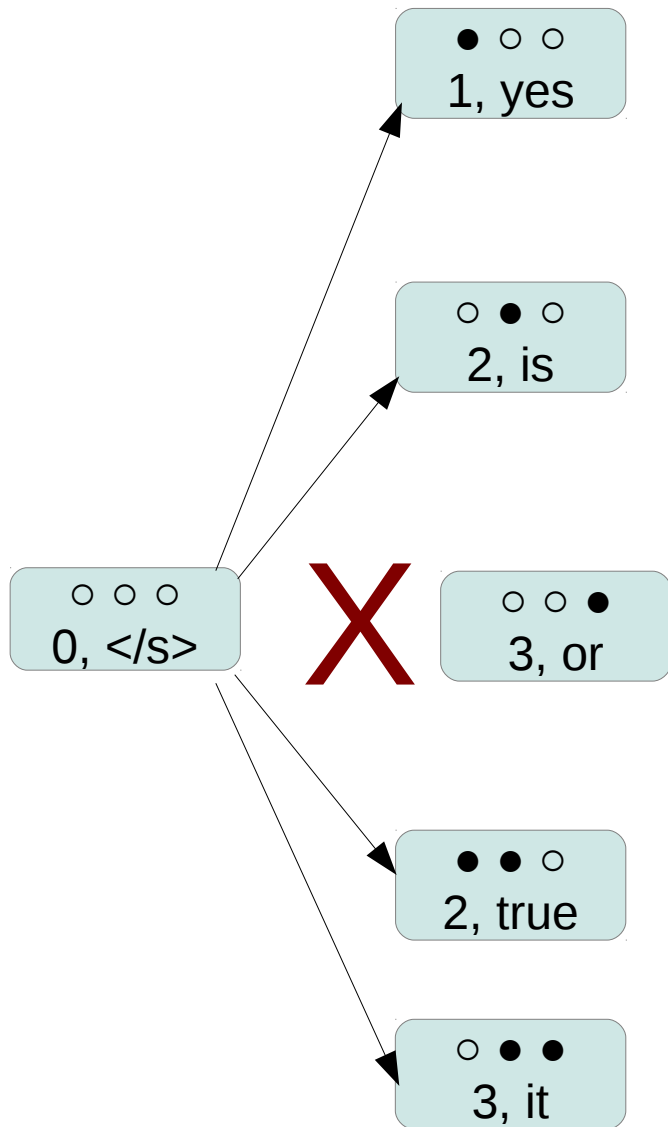
● ● ● ○  
2, true

● ● ● ○  
1, yes

● ● ● ○  
3, or

# Max Distortion Example

そう	です	か
yes	is	or
that's true		
is it		



If distortion limit is “1”, then this hypothesis has distortion of 2, and will never be expanded



# Evaluation

# Evaluation

- We built a machine translation system, we need to know:
  - **How good** is our system?
  - Is system A **better than** system B?
  - What are the **problems** with our system?

# Human Evaluation

- **Adequacy:** Is the meaning correct?
- **Fluency:** Is the sentence natural?
- **Pairwise:** Is X a better translation than Y?

太郎が花子を訪問した


 Taro visited Hanako    the Taro visited the Hanako    Hanako visited Taro

Adequate?	○	○	×
Fluent?	○	×	○
Better?	B, C	C	

# Automatic Evaluation

- How well does the translation match a reference?
  - (or multiple references: more than one correct translation)
- **BLEU**: n-gram precision, brevity penalty [Papineni 03]

Reference: Taro visited Hanako

System: the Taro visited the Hanako

1-gram: 3/5

2-gram: 1/4

Brevity:  $\min(1, |\text{System}|/|\text{Reference}|) = \min(1, 5/3)$

brevity penalty = 1.0

$$\begin{aligned}\text{BLEU-2} &= (3/5 * 1/4)^{1/2} * 1.0 \\ &= 0.387\end{aligned}$$

- Also **METEOR** (normalizes synonyms), **TER** (# of changes), **RIBES** (reordering)

# Assignment

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- (Only one assignment this week)
- You are given a baseline machine translation system
  - **LM/Alignment:** Baseline from exercises 1, 2
  - **TM:** Phrases of up to length 4
  - **SM:** Uniform distribution
  - **RM:** Distortion penalty
  - **Reordering Limit:** 6
- Try to improve its accuracy by changing one of the features listed above, or anything else

# Assignment Details

- Download the exercise from the web
- You can find a list of commands to run in `run-translate.sh`
- Send any files you changed, BLEU score before/after, and a short description of the change
  - Due date: February 12th, 23:59
  - Address: [neubig@is.naist.jp](mailto:neubig@is.naist.jp)